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COMPUTATION OF CONTINUOUS DECOMPRESSION SCHEDULES FOR DEEP SEA DIVES

JAMES S. ROBERTSON

AND

GEORGE MOELLER



March 1968

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COMPUTATION OF CONTINUOUS DECOMPRESSION SCHEDULES FOR DEEP SEA DIVES

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ABSTRACT

A digital computer program for calculating either continuous ascent or stop-type decompression schedules is described, and examples of applications are given. The formulas used for continuous ascent were obtained analytically as solutions of differential equations relating the inert gas tension in the current critical tissue to the safe depth and with the actual depth kept equal to the safe depth at all times after an initial fast rise from the bottom to the safe depth. Thus the rate of decompression of the critical tissue controls the rate of ascent. Gas tensions in nine tissues having the same range of gas exchange half-times as have been used in EDU reports are calculated on a continuous basis, with the one having the deepest safe depth being the current critical tissue. The stop-type ascent portion of the program may be used to generate a staged ascent using the same parameters for comparison with the continuous ascent schedule. The starting conditions for ascent may either be computed by the program from the dive history or be communicated to it as a subroutine in connection with another program. The program may be used either to prescribe ascent schedules or to analyze dives for which the history is known.

CONTENTS

Introduction	1
Mathematical Basis	2
General	2
Safe Depth	2
Ascent Formulas	3
Constant Rate	3
Intersection of Fast Ascent and Safe Depth Curves	4
Variable Ascent Rate	4
Change of Critical Tissue	6
Program Description	6
Input - Output	7
Input	7
Output	7
Applications	8
Discussion	9
References	10
Appendix A Principal Variables	10
Appendix B	12
1 Listings	12
2 Data Deck	22
Appendix C Computer Output	22

COMPUTATION OF CONTINUOUS DECOMPRESSION SCHEDULES FOR DEEP SEA DIVES

INTRODUCTION

Too rapid ascent from prolonged deep dives can result in decompression sickness or "the bends," an illness associated with inert gas bubble formation in the blood and tissues of the body. This illness is preventable through the use of appropriate decompression schedules, which depend principally on the dive depth and its duration. However, many other factors that may affect the diver's physiology, such as exercise, water temperature, and the effects of breathing different gas mixtures, must also be considered in constructing decompression schedules. A panoramic view of recent work in diving physiology is presented in a book edited by Lambertsen.¹

Workman² has critically reviewed the development of the U.S. Navy's current decompression schedules.³ These are based on the principles of inert gas exchange as developed by Haldane and co-workers,⁴ and on their determination of the amounts by which the inert gas tensions in the tissues may safely exceed the ambient pressure without producing the bends.

The currently used decompression schedules involve a series of steps, or stages, at intervals of 10 ft of depth. The diver waits at each stage until it is safe for him to be at the next stage, at which time he ascends to it, and so on, until the surface is reached. These schedules have been constructed to minimize the decompression time, consistent with preventing the bends, and have been proved safe in thousands of real dives. However, it is apparent that any staged decompression schedule is inherently less than optimal, because as soon as the diver has been at a given stage for even a short time, it would be safe for him to be at some shallower depth, which in turn would give an increase in the outgassing pressure gradient and a shortening of the time required for further decompression. At the deeper stages, particularly in dives with short bottom times, some tissues may actually still be absorbing rather than releasing inert gases, thus

obligating longer stops at subsequent stages. The importance of this effect increases with the dive depth, but decreases with increasing bottom time.

The potential advantages of continuous, rather than staged, ascent schedules have previously been recognized, for example, by Workman² and Bradner and Mackay.⁵ Shreiner and Kelly⁶ have developed continuous decompression formulas assuming constant excess saturation pressure, both for constant partial pressures of oxygen and for constant percentage of oxygen in the breathing mixture.

The purposes of this report are (1) to present the derivation of a set of formulas obtained as solutions of differential equations that include the assumption that the depth is continuously changing in such a way as to keep the diver exactly at his current safe depth, and (2) to describe a digital computer program, SIMDIVE, that has been developed to use the above method in the development of more nearly optimal decompression schedules.

In this derivation, we do not consider the elaborate mechanisms involved in bubble formation, but work from the same assumptions used in developing the standard tables, to the effect that, for any particular inert gas partial pressure in a tissue, there is some corresponding minimal external pressure that is sufficient to prevent bubble formation.² The depth associated with this minimal pressure is designated the safe depth.

During the decompression process the gases are eliminated from the body and the required external pressure decreases. The formulas developed for the SIMDIVE program combine the equations for the rates of uptake and release of inert gases with equations relating the internal partial pressures to the safe depth. A schedule is produced such that, after an initial rapid ascent to the safe depth, the actual depth is kept equal to the instantaneous value of the safe depth.

The formulas developed by the above methods are used in a computer subroutine called ASCENT. ASCENT is designed to be called by SIMDIVE or an-

other main program such as Moeller's STANDIVE⁷ that supplies the parameters and constants needed to express the conditions of the dive and the diver's status with respect to his tissue inert gas partial pressures at the beginning of the ascent. Another subroutine, DESCENT, provides an alternative method for generating the ascent starting conditions from the dive history.

The SIMDIVE program and associated subroutines were originally written in FORTRAN II for compatibility among the Honeywell-800 at the SMC and the IBM-7094 and the CDC-6600 computers at BNL. However, the version presented in this report includes some FORTRAN IV features adapted principally for use with the CDC-6600 computer.

MATHEMATICAL BASIS

It is assumed that the driving force for gas exchange is the partial pressure gradient between the breathing gas mixture and the gas tension in the tissues. For each tissue a rate-limiting gas exchange factor, λ , may be assigned. This factor lumps the effects of several parameters. It depends primarily upon the blood perfusion rate per gram of tissue and the solubility of the gas under consideration in the tissue relative to that in the blood, but also reflects variations in diffusion rates for the gases and the effects of temperature changes. The λ 's are related to tissue gas exchange half-times through the relationship $\lambda T = \log_e 2$. The various tissues are regarded as being in parallel for gas exchange considerations, and thus are treated independently. For consistency with other work^{2,7} nine tissues having a spectrum of λ 's corresponding to gas exchange half-times ranging from 5 to 240 min are used. These half-times were arbitrarily chosen to give the desired spread of values, and do not necessarily correspond to any particular anatomical tissues or organs. The factors relating tissue gas tensions to the safe depth are also functions of the half-times. Because of the different rates of uptake and release of the gases among the tissues, there will usually be one for which the safe depth at a given moment is greatest, and this will be called the critical tissue. If two or more tissues tie for this distinction, the one with the longer half-time is taken.

The plan for ascent is first to ascend as rapidly as is practical (60 ft/min) until the actual depth equals the safe depth for the critical tissue. From

this time on, the actual depth is kept equal to the safe depth for the current critical tissue. Control passes from one tissue to the next when the curves representing their individual safe depths cross. One of the programming problems, as discussed below, is to predict the time for changing the critical tissue. For dives involving short bottom times, the rapidly exchanging tissues are the controlling ones at the beginning of ascent, and control passes to progressively slower tissues as the surface is approached. For very prolonged dives, the slower tissues may be rate-controlling from the beginning of ascent.

For comparison, a variation of the program produces a staged ascent. In this variation the diver remains at a given stop until a time such that by ascending to the next even 10-ft level, at the maximum rate, he will arrive at the new depth at the instant this becomes his safe depth. This is slightly different from the standard tables, in which the ascent time is not considered, but gives a fairer comparison with the continuous method.

The notation to be used is given in Table 1.

Insofar as possible, the derivations that follow are in terms of a single tissue, and, for simplicity of expression, subscripts are omitted when possible without ambiguity. In the computer program the subscripts are needed to distinguish among the various tissues and gases.

General

If $(P - Q)$ is the driving force and λ is the rate-limiting factor for inert gas exchange, then

$$\frac{dQ}{dt} = \lambda(P - Q), \quad (1)$$

or, in standard linear equation form,

$$\frac{dQ}{dt} + \lambda Q = \lambda P, \quad (2)$$

also

$$AD = AD_0 - DD = AD_0 - \int_0^t R dt, \quad (3)$$

$$P = G(AD + 33) = G\left(D - \int_0^t R dt\right) \quad (4)$$

Safe Depth

Workman² mentions several formulas that have been used to calculate safe inert gas partial pressures in tissues for given depths. In the present no-

Table 1

Symbol	Explanation	Units
$Q(J,I)$	I th gas tension in J th tissue (range for I , 1-3, for J , 1-9)	ft of water
$Q(L,I)$	I th gas tension in critical tissue, L ($I=1$ is used for total inert gas tension, $I=2$ for nitrogen, and $I=3$ for helium)	ft of water
$Q(J,I)_0$	$Q(J,I)$ at start of current step	ft of water
$Q(J,I)_s$	Safe value for $Q(J,I)$ at current depth	ft of water
$P(I)$	Partial pressure of I th gas in breathing mixture	ft of water
$G(I)$	Fraction of I th gas in breathing mixture	—
t	Time from start of current step	min
R	Rate of change of depth, taken as positive for ascent	ft/min
AD	Actual depth (gauge)	ft of water
$SD(J)$	Safe depth for J th tissue (gauge)	ft of water
AD_0	Depth at start of current step (gauge)	ft of water
DD	$AD_0 - AD = \int_0^t R dt$, change of depth for step	ft of water
D	$AD_0 + 33$, total external pressure	ft of water
$\lambda(J)$	Turnover rate constant for J th tissue, $\lambda = (\log_e 2)/\text{half-time}$	min ⁻¹
$AK(J)$	$Q(J,I)_s$ at surface	ft of water
$AC(J)$	$\Delta AK(J)/\text{ft of depth}$	—

NOTE All depths and pressures are measured in feet of sea water, absolute, unless gauge depth is specified. (For fresh water dives $D = AD_0 + 34$, and the AK 's and AC 's are multiplied by 1.025, the density of sea water.)

tation, the following formula is equivalent to the one used for constructing the tables of recommended M values in ref (2)

$$Q_s = AK + AC \cdot AD \quad (5)$$

By rearrangement of Eq (5), the safe depth for a given value of Q is

$$SD = (Q - AK)/AC \quad (6)$$

Thus, if Q changes, the SD changes proportionally

$$\begin{aligned} SD_0 - SD &= \frac{(Q_0 - AK)}{AC} - \frac{(Q - AK)}{AC} \\ &= \frac{(Q_0 - Q)}{AC}, \end{aligned} \quad (7)$$

or,

$$SD = SD_0 - \frac{(Q_0 - Q)}{AC} \quad (8)$$

Ascent Formulas

As mentioned above, the ascent schedule has two phases, first a rapid ascent to the minimum safe depth, then a slower ascent maintaining the current safe depth. The former involves a constant rate of change of depth, whereas the latter involves a continuously changing rate. The formulas for constant rate are simpler and are derived first. These formulas are also used for descent and for computing staged ascent schedules.

Constant Rate

With R constant,

$$\int_0^t R dt = Rt, \quad (9)$$

Therefore, substitution of Rt into Eq (4) gives

$$P = G(D - Rt), \quad (10)$$

and Eq (2) becomes

$$\frac{dQ}{dt} + \lambda Q = \lambda G(D - Rt), \quad (11)$$

for which the solution is*

$$Q = \exp(-\lambda t) \left[\int_0^t \lambda G(D - Rt) \exp(\lambda t) dt + C \right] \quad (12)$$

Integration and simplification, with $C = Q_0$, yield

$$\begin{aligned} Q &= GD[1 - \exp(-\lambda t)] - \frac{GR[\lambda t - 1 + \exp(-\lambda t)]}{\lambda} + \\ &\quad Q_0 \exp(-\lambda t) \end{aligned} \quad (13)$$

In this form it is seen that the third term on the right represents the function Q for $G=0$, i.e., if the diver breathes pure oxygen. Similarly, the first term represents the build-up in tissue inert gas partial pressure that would occur if $R=0$ and $Q_0=0$. The middle term corrects for the effect of

*The symbolism $\exp(X)$ is used here to represent e^X , where e is the base of the natural logarithms, 2.718.

the rate of ascent. For computing purposes, a rearrangement of Eq. (13), with the exponential terms collected, is used

$$Q = GD - \frac{GR(\lambda t - 1)}{\lambda} + \left(Q_0 - GD - \frac{GR}{\lambda} \right) \exp(-\lambda t) \quad (14)$$

For constant depth, with $R = 0$, Eq. (14) becomes

$$Q = GD + (Q_0 - GD) \exp(-\lambda t) \quad (15)$$

The time required for Q to reach some other value, Q_t , at constant depth may be calculated by solving Eq. (15) for t

$$t = \frac{\log_e[(Q_0 - GD)/(Q_t - GD)]}{\lambda} \quad (16)$$

provided that $GD \leq Q_t \leq Q_0$ or $Q_0 \leq Q_t \leq GD$

Intersection of Fast Ascent and Safe Depth Curves

To find the time of intersection of the fast ascent and safe depth curves, we set

$$AD = SD \quad (17)$$

and substitute Eq. (3) and Eq. (8)

$$AD_0 - Rt = SD_0 - \frac{(Q_0 - Q)}{AC} \quad (18)$$

But, from Eq. (13),

$$(Q_0 - Q) = (Q_0 - GD)[1 - \exp(-\lambda t)] + \frac{GR[\lambda t - 1 + \exp(-\lambda t)]}{\lambda} \quad (19)$$

Substitution of the right-hand member of Eq. (19) into Eq. (18) eliminates Q and gives an expression involving only t and variables whose values are known at the start of a given step. Although this expression cannot be solved analytically for t , a value of t may be obtained to any desired accuracy through successive iterations of Newton's approximation formula.⁸

If it is desired to solve $F(t) = 0$ for t ,

$$t \approx t_0 - \frac{F(t)}{F'(t)}, \quad (20)$$

where t_0 is an initial guess for t , and $F'(t) = dF(t)/dt$. The approximation obtained by the first solution of Eq. (20) for t is used as the t_0 for the next iteration, etc., until the answer converges within the desired limits. Thus t is obtained from successive iterations of

$$t = t_0 - \frac{AD_0 - SD_0 - Rt + \{(Q_0 - GD)[1 - \exp(-\lambda t)] + GR[\lambda t - 1 + \exp(-\lambda t)]/\lambda\}/AC}{-R + \{\lambda(Q_0 - GD)\exp(-\lambda t) + GR[1 - \exp(-\lambda t)]\}/AC} \quad (21)$$

The first t_0 is obtained by substituting the approximation

$$\exp(-\lambda t) \approx 1 + \lambda t - \frac{1}{2}(\lambda t)^2 \quad (22)$$

into Eq. (19), and the result into Eq. (18), and solving the resulting quadratic expression for t . In subroutine ASCENT, the critical tissue at the time of intersection is determined by selecting the tissue for which the substitution involving Eq. (22) gives the least value for t , then the exact value of t is calculated for the critical tissue only, by using Eq. (21). When the diver's actual depth equals his safe depth, another set of equations involving the use of a variable ascent rate is needed. The derivations for these equations follow.

Variable Ascent Rate

To maintain $AD = SD(L)$,

$$R = \frac{dSD(L)}{dt} = -\frac{dQ(L,1)}{dt} / AC(L), \quad (23)$$

and

$$DD = \int_0^t R dt = \frac{[Q(L,1)_0 - Q(L,1)]}{AC(L)} \quad (24)$$

Substitution of Eq. (24) into Eq. (4) gives

$$P = G \left[D - \frac{[Q(L,1)_0 - Q(L,1)]}{AC(L)} \right], \quad (25)$$

and Eq. (2) becomes

$$\begin{aligned} & \frac{dQ(J,I)}{dt} + \lambda_J Q(J,I) \\ &= \lambda_J G_I \left[D - \frac{[Q(L,1)_0 - Q(L,1)]}{AC(L)} \right] \end{aligned} \quad (26)$$

In order to obtain an integrable form of Eq. (26), it is necessary first to solve for $Q(L,1)$. With the understanding that only the total inert gas tension in the critical tissue, $Q(L,1)$, is under consideration, the notation may be simplified

$$\frac{dQ}{dt} + \lambda Q = \lambda G \left(D - \frac{Q_0}{AC} \right) + \frac{\lambda G Q}{AC}, \quad (27)$$

or, in standard form

$$\frac{dQ}{dt} + \left(1 - \frac{G}{AC} \right) \lambda Q = \lambda G \left(D - \frac{Q_0}{AC} \right) \quad (28)$$

In Eq (28), let

$$K_1 = \left(1 - \frac{G}{AC}\right) = \frac{AC - G}{AC},$$

$$K_2 = G\left(D - \frac{Q_0}{AC}\right),$$

$$K_3 = \frac{K_2}{K_1} = \frac{G(D - AC - Q_0)}{AC - G}$$

Then

$$\frac{dQ}{dt} + \lambda K_1 Q = \lambda K_2 \quad (29)$$

Solving Eq (29) gives

$$Q = \exp(-\lambda K_1 t) \left[\int_0^t \lambda K_2 \exp(\lambda K_1 t) dt + C \right] \quad (30)$$

Integrating between limits gives

$$Q = \exp(-\lambda K_1 t) \left\{ \frac{\lambda K_2}{\lambda K_1} [\exp(\lambda K_1 t) - 1] + C \right\} \quad (31)$$

For $t=0$, $C=Q_0$,

$$Q = K_3 [1 - \exp(-\lambda K_1 t)] + Q_0 \exp(-\lambda K_1 t) \quad (32)$$

$$= K_3 + (Q_0 - K_3) \exp(-\lambda K_1 t) \quad (33)$$

for $Q(L,1)$, i.e., the total inert gas tension in the critical tissue [Eq (33) is not directly applicable for other tissues or for individual inert gases]

From Eqs (3), (24), and (33), we obtain

$$DD = (Q_0 - K_3) [1 - \exp(-\lambda K_1 t)] / AC \quad (34)$$

To solve Eq (34) for t , let

$$K_4 = (Q_0 - K_3) / AC,$$

then

$$t = -\log_e(1 - DD/K_4) / \lambda K_1 \quad (35)$$

Thus at this point, for the critical tissue, L , we have analytical solutions for Q , R , and DD as functions of time, and for time as a function of the change in depth, DD , all with $AD=SD$. Whether Eq (34) or Eq (35) is to be used depends on whether t or DD is known, respectively. We proceed to solve Eq (26) for the other tissues and for the component inert gases.

From Eq (33),

$$\begin{aligned} & Q(L,1)_0 - Q(L,1) \\ &= [Q(L,1)_0 - K_3] [1 - \exp(-\lambda L K_1 t)] \quad (36) \end{aligned}$$

Substitution of the right-hand member of Eq (36) into Eq (26) gives

$$\begin{aligned} & \frac{dQ(J,I)}{dt} + \lambda_J Q(J,I) \\ &= \lambda_J G_I \left\{ D - \frac{[Q(L,1)_0 - K_3] [1 - \exp(-\lambda_L K_1 t)]}{AC(L)} \right\} \end{aligned} \quad (37)$$

From the definition of K_3 it is readily shown that

$$\frac{Q_0 - K_3}{AC} \equiv \frac{G_1 D - K_3}{G_1} \quad (38)$$

With this substitution, Eq (37) reduces to

$$\begin{aligned} & \frac{dQ(J,I)}{dt} + \lambda_J Q(J,I) \\ &= \lambda_J G_I \left[\frac{K_3}{G_1} + \left(D - \frac{K_3}{G_1} \right) \exp(-\lambda_L K_1 t) \right] \end{aligned} \quad (39)$$

with the solution

$$\begin{aligned} Q(J,I) &= \exp(-\lambda_J t) \left\{ \int_0^t \lambda_J G_I \left[\frac{K_3}{G_1} + \frac{G_1 D - K_3}{G_1} \exp(-\lambda_L K_1) \right] \exp(\lambda_J t) dt + C \right\} \end{aligned} \quad (40)$$

Integration of Eq (40) gives

$$\begin{aligned} Q(J,I) &= \exp(-\lambda_J t) \left\{ \frac{\lambda_J G_I}{G_1} \left(\frac{K_3}{\lambda_J} [\exp(\lambda_J t) - 1] + \frac{G_1 D - K_3}{\lambda_J - \lambda_L K_1} \{ \exp[(\lambda_J - \lambda_L K_1)t] - 1 \} \right) + C \right\}, \end{aligned} \quad (41)$$

$$\begin{aligned} Q(J,I) &= \frac{G_I}{G_1} \left\{ K_3 [1 - \exp(-\lambda_J t)] + \frac{\lambda_J (G_1 D - K_3)}{\lambda_J - \lambda_L K_1} [\exp(-\lambda_L K_1 t) - \exp(-\lambda_J t)] \right\} + C \exp(-\lambda_J t) \end{aligned} \quad (42)$$

for $t=0$, $C=Q(J,I)_0$

Finally

$$\begin{aligned} Q(J,I) &= \frac{G_I}{G_1} \left[K_3 + \frac{\lambda_J (G_1 D - K_3)}{\lambda_J - \lambda_L K_1} \exp(-\lambda_L K_1 t) \right] + \\ & \left[Q(J,I)_0 - \frac{G_I}{G_1} \left(K_3 + \frac{\lambda_J (G_1 D - K_3)}{\lambda_J - \lambda_L K_1} \right) \right] \exp(-\lambda_J t) \end{aligned} \quad (43)$$

An indeterminacy arises in Eq (42) if $\lambda_J = \lambda_L K_1$, with

$$\frac{\exp(-\lambda_L K_1 t) - \exp(-\lambda_J t)}{\lambda_J - \lambda_L K_1} = \frac{0}{0} \quad (44)$$

This indeterminacy may be removed through an application of L'Hopital's rule

$$\lim_{\lambda_J \rightarrow \lambda_L K_1} \left| \frac{\exp(-\lambda_L K_1 t) - \exp(-\lambda_J t)}{\lambda_J - \lambda_L K_1} \right| = t \exp(-\lambda_L K_1 t) \quad (45)$$

In ASCENT, a modification of Eq. (43) involving substitution of Eq. (45) is used if

$$|\lambda_J - \lambda_L K_1| < 10^{-6}$$

Otherwise an expression equivalent to Eq. (43) is used

Change of Critical Tissue

Except in saturation dives, when the critical tissue is the one with the longest half-time, the critical tissue changes whenever the safe depth curve of one of the slower tissues crosses that of the current critical tissue. It is useful to be able to predict when this will occur, and this may be done through the use of the formulas derived below.

The critical tissue changes when, for $J > L$ (assuming that the tissues are ordered by increasing half-times),

$$SD(J) = SD(L) \quad (46)$$

From Eq. (8),

$$\begin{aligned} SD(J)_0 - \frac{[Q(J)_0 - Q(J)]}{AC(J)} \\ = SD(L)_0 - \frac{[Q(L)_0 - Q(L)]}{AC(L)}, \end{aligned} \quad (47)$$

$$\begin{aligned} SD(L)_0 - SD(J)_0 + \frac{[Q(J)_0 - Q(J)]}{AC(J)} - \\ \frac{[Q(L)_0 - Q(L)]}{AC(L)} = 0 \end{aligned} \quad (48)$$

Substitution from Eq. (36) and Eq. (43) with $G_I = G_1$ gives

$$\begin{aligned} SD(L)_0 - SD(J)_0 + \\ \frac{[Q(J)_0 - K_3][1 - \exp(-\lambda_J t)] + \frac{\lambda_J(GD - K_3)}{\lambda_J - \lambda_L K_1}[\exp(-\lambda_L K_1 t) - \exp(-\lambda_J t)]}{AC(J)} - \frac{[Q(L)_0 - K_3][1 - \exp(-\lambda_L K_1 t)]}{AC(L)} = 0 \end{aligned}$$

Again, Eq. (49) cannot be solved explicitly for t , but a numerical solution is obtainable by the same method as used above for the fast intersection. If $F(t)$ is the left member of Eq. (49),

$$F'(t) = \frac{[Q(J)_0 - K_3]\lambda_J \exp(-\lambda_J t) + \frac{\lambda_J(GD - K_3)}{\lambda_J - \lambda_L K_1}[\lambda_J \exp(-\lambda_J t) - \lambda_L K_1 \exp(-\lambda_L K_1 t)]}{AC(J)} - \frac{[Q(L)_0 - K_3]\lambda_L K_1 [\exp(-\lambda_L K_1 t)]}{AC(L)}$$

and

$$t \approx t_0 - \frac{F(t)}{F'(t)} \quad (51)$$

In this case a satisfactory first estimate for t_0 is obtained by substituting the approximation

$$\exp(X) \approx 1 + X \quad (52)$$

into Eq. (49) and solving for t

$$t_0 = \frac{[SD(L)_0 - SD(J)_0]}{\left[\frac{Q(L)_0 - G_1 D}{AC(L)} \lambda_L - \frac{Q(J)_0 - G_1 D}{AC(J)} \lambda_J \right]} \quad (53)$$

The same expression for t_0 is obtained if the time of intersection of the tangents at $t=0$ for the two curves, $SD(J)$ and $SD(L)$ as defined by Eq. 8, is taken

PROGRAM DESCRIPTION

Listings and logic diagrams for program SIMDIVE and its subroutines are given in Appendix B.

As the "main" program, SIMDIVE reads in the initializing data and calls the appropriate subroutines. The first two columns of the first card of a data deck determine whether the run will begin with DESCENT or will go directly to ASCENT, and whether new half-time, AK , AC , and gas mixture parameters or those for the preceding deck are to be used. The balance of this card through column 72 may be used to give any alphanumeric information desired to identify the dive. (For consistency with other reports, the half-times for nine tissues usually used are 5, 10, 20, 40, 80, 120, 160, 200, and 240 min.) If DESCENT is used, and the diver is not at the surface when the END card is reached, the program automatically proceeds with ASCENT without first returning to SIMDIVE. When the surface has been attained in ASCENT, there is a return to SIMDIVE, which proceeds to call TABLE and PLOT, then starts over or stops, depending on whether another dive follows.

Subroutine DESCENT is used primarily to compute the inert gas partial pressures in the tissues at the beginning of ASCENT. For each step it reads in the time and depth for the end of the step and the index for the gas mixture used during the step. (In an alternative version, the actual gas mixture fractions are read in here.) The starting time and depth for a given step are assumed to be those for the end of the immediately prior step. Subroutine TENSION is called for computing the inert gas partial pressures in the tissues at the end of each step. DESCENT may also be used to compute the safe depths, partial pressures, and safe partial pressures for the decompression steps in any dive in which the rates of change of depth are all constants. Finally, DESCENT may be used to study the continuation of the decompression process after the diver has surfaced, for example, to obtain the starting partial pressures in the tissues for repetitive dives.

ASCENT may be used as an independent subroutine, or may be joined with DESCENT, as is done in the listing given in Appendix B. ASCENT inserts a dummy first step of zero duration to print out the starting conditions for ascent. It automatically determines the gas mixture to use, based on the starting depth for each step. The safe depths for all nine tissues are computed, and the tissue having the greatest safe depth is selected as the critical tissue. If the distance from the actual depth to the safe depth for the critical tissue is >0.01 ft, the program calls subroutine FASTRIZ, which takes the diver to the current safe depth. Otherwise the slow ascent method is used, in which the actual depth and safe depth are kept equal. Normally a step is an interval of 10 ft, but if a change of critical tissues or a gas mixture boundary is encountered first, the information as of the intervening depth is printed out. If the rate of ascent is >10 ft/min, ascent proceeds for 1 min rather than 10 ft for that step. In the printout the critical tissue for the step is marked with an asterisk. If the "stop" is due to a change in critical tissue, the next critical tissue is also marked.

Subroutine FASTRIZ finds the time of intersection of the actual depth curve with the safe depth curve, assuming ascent at the maximum rate, which is taken as 60 ft/min unless another value is read in by SIMDIVE.

Subroutine PLOT produces a graph of the DESCENT-ASCENT depth-time curve. The ordinate scale is based on MAXDEEP. A caption and ordinate labels for 0, $\frac{1}{4}$, $\frac{1}{2}$, $\frac{3}{4}$, and 1 times MAXDEEP are

printed out. The time scale is adjusted to keep the plot on two pages, through factors entered as DATA statements. Once the scales have been determined, PLOT proceeds by treating each line of printout as a time interval, and examining the end times for the dive steps in sequence. If a step end time falls within the current time interval, the corresponding POINT is labeled with an asterisk. When a step is encountered that is later than the current time interval, this interval is printed out, the labels for the steps that fell within the interval are "erased" (i.e., labeled blank), and the program proceeds to the next time interval. For intervals containing points printed out, the time of the last point in the interval is printed. After the last step of the dive, the ordinate scales and captions are printed out again.

Subroutine TABLE lists the starting and ending time and depth and the gas mixture for each step. The times are converted from minutes to hours and minutes for use in TABLE.

Subroutine TENSION uses the constant rate formula, Eq. (14), for computing the inert gas partial pressures in the tissues.

INPUT-OUTPUT

Input

The input data deck is described in Table 2.

Output

SIMDIVE assigns consecutive serial numbers to the dives in a given run. This dive number, the identification field of card 1, and the date of the run are printed at the beginning of the output, before TABLE and before PLOT. If they are new parameters, H, AK, and AC are printed. For DESCENT, the dive number, step number, prior depth, end-of-step depth, oxygen, nitrogen, and helium percentages, safe tissue pressures and Q values (total inert, nitrogen, and helium) for each of nine tissues, the step time interval, the cumulative dive time, the rate of ascent, and the safe depth for the critical tissue are printed out for each step. The critical tissue is marked with an asterisk. For ASCENT, the first five gas mixtures (oxygen, total inert, nitrogen, and helium) and the depths for which each is to be used, and the maximum rate of ascent are printed out. The dive number, etc., as listed for DESCENT are printed except that the Q values are followed by the step time interval, the cumulative ascent time, the cumulative dive time, and the average ascent rate for each step, instead of the items listed for DESCENT. Since the actual

Table 2

<u>Input data deck</u>	<u>Entry</u>	<u>Meaning</u>
Card 1 Col 1	Blank or 0 1	Use preceding parameters Read new parameters (Cards 2-14)
Col 2	Blank, 0, or 1 2 3	CONTINUOUS ASCENT only DESCENT, then continuous ASCENT DESCENT, then staged ASCENT
Col 3-72	Alphanumeric	Dive identification
If col 1, card 1 blank or zero, skip to card 15		
Card 2 8x 9F8 0	Real type numbers	$H(J), J=1,9$
Card 3 8x 9F8 0	" " "	$AC(J), J=1,9$
Card 4 8x 9F8 0	" " "	$AK(J), J=1,9$
Cards 5-14 Col 9-16	" " "	Nitrogen, GMIX(3,J)
Col 17-24	" " "	Helium, GMIX(4,J), $J=1,10$
Card 15 Col 17-24	" " "	Initial time, $T(1)$
Col 25-32	" " "	Initial depth, DEPTH(1)
Col 33-37	Integer	MAXOEEP (for scaling ordinate)
Col 38-45	Real type number	RATE (maximum ascent rate)
Cards 16-18 8x 9F8 4	" " "	Initial tissue pressures, $Q(I,J), I=1,9, J=1,3$
If col 2, card 1 blank, 0, or 1, skip to card $N+2$		
Cards 19- N^* Col 1-3	Blank	
Col 4-8	Real type number	End of step hour
Col 9-13	" " "	End of step minute
Col 14-20	" " "	End of step depth
Col 46-50	Integer 1-10	Index for step GMIX
Card $N+1$ Col 1-3	END	Indicates end of DESCENT deck
Card $N+2$ Card 1 of next data deck or end of file card		

* N may be any number 19-217, with one card per step in DESCENT

depth and the safe depth are kept equal after the initial fast ascent, the safe depth is not printed separately

After the diver has surfaced, or the 198th step, a tabulation of the step numbers, step times, beginning and end-of-step depths, beginning and end-of-step times, and the gas mixture for each step are printed by subroutine TABLE

Subroutine PLOT prints a graph of depth vs time for the dive

Execution time of the program on the CDC-6600 averages about 2 sec per dive for the 600-ft dives

APPLICATIONS

Figure 1 compares two ascent schedules, one for staged ascent and the other for continuous ascent, both as calculated with the SIMDIVE program following descent to 450 ft for 1 hr In both dives it is assumed that the breathing gas mixture is air

during descent to 75 ft, then 96% helium, 4% oxygen for the rest of descent, while at 450 ft, and during ascent to 200 ft, after which air is again used Although there is very little difference between the two schedules for the early stages, the difference gradually accumulates, and the diver surfaces 2 hr sooner by the continuous method

In Figure 2 the standard table schedule for a dive to 190 ft for 1 hr on air is compared with ascent schedules calculated by the SIMDIVE staged and continuous methods Although the SIMDIVE staged schedule moves through the deeper stages a few minutes slower than does the standard table, it suggests that less time is needed at the 10-ft stage and that the diver could surface about 20 min sooner Use of the continuous schedule would save another 20 min in this dive

In Figure 3 a schedule for ascent as computed by the SIMDIVE method is compared with the schedule given in the diving manual table for ex-

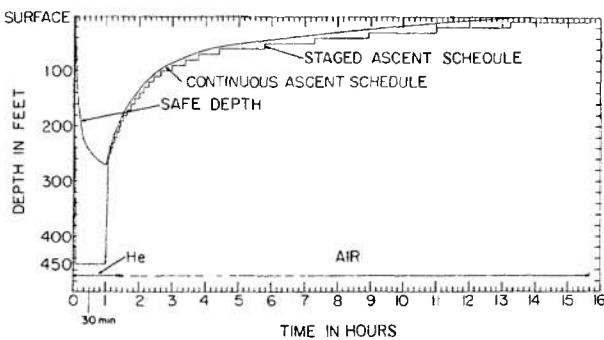


Figure 1 Comparison of staged and continuous ascent schedules, both as calculated by SIMDIVE for a helium dive to 450 ft for 60 min

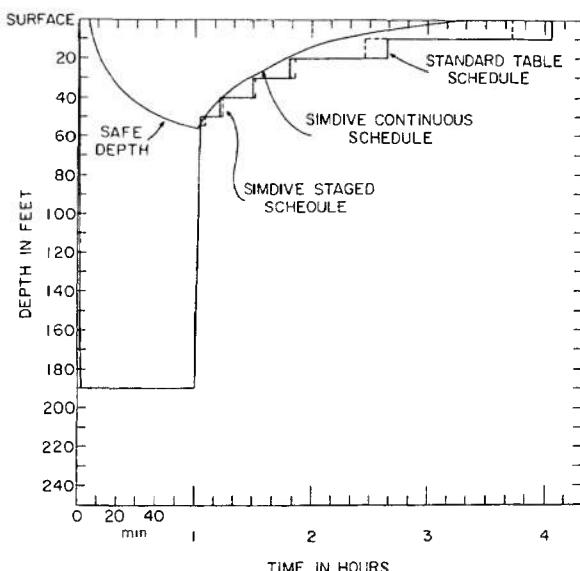


Figure 2 Comparison of staged and continuous schedules calculated by SIMDIVE with the staged schedule from the standard tables for a dive to 190 ft for 60 min on air

treme exposures^{3,p 103} for decompression following an air dive to 300 ft for 3 hr. Here it is seen that for the shallow stages the safe depth as calculated by the present method, and assuming that the diving manual schedule is being followed, is in close agreement with the depths prescribed in the standard tables. However, there is a large difference at the deep stages. Thus the difference between the two schedules is due more to the different relationship assumed between tissue tension and the safe depth for the deep stages than to the difference between staged and continuous ascent schedules.

Figure 4 shows a family of continuous ascent schedule curves for dives to 600 ft for various bot-

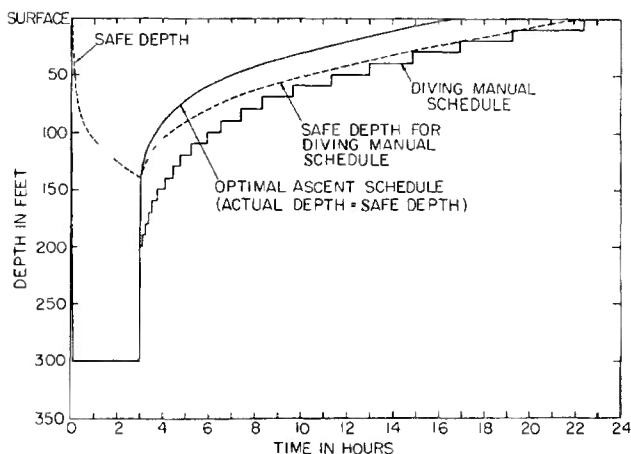


Figure 3 Comparison of continuous ascent schedule calculated by SIMDIVE with the corresponding schedule from the diving manual for a dive to 300 ft for 180 min on air

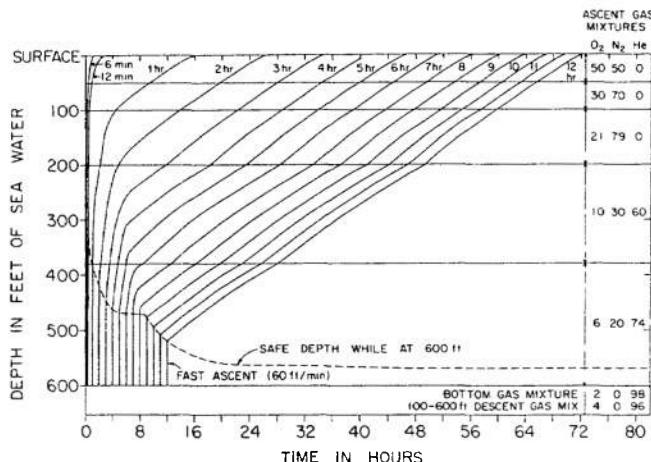


Figure 4 Continuous ascent schedules for mixed gas dives to 600 ft

tom times ranging from 6 min to 12 hr. The gas mixtures used are tabulated at the right-hand side of the graph. Changes in the gas mixtures account for some of the sharp changes in slope, while change of critical tissue accounts for others. As the 240-min half-time tissue becomes more nearly saturated, it becomes the critical tissue earlier in ascent. After about 20 hr bottom time, further increases in bottom time do not increase the ascent times.

DISCUSSION

The above derivations provide the formulas needed for producing any desired decompression schedule, either with staged ascent or with a con-

tinuous ascent in which the actual depth is kept equal to the minimum safe depth at all times after an initial fast ascent to the safe depth, with the assumption that the safe total inert gas partial pressure in the critical tissue is linearly related to the depth according to Eq. (5). If some other relationship is required, the formulas will have to be modified accordingly. Other possible improvements include increasing the number of tissues considered, or even using a continuous spectrum of gas exchange half-times. Either of these changes would produce a somewhat smoother schedule than does the present method, in which the rate changes abruptly when the critical tissue changes.

The schedules produced by the present method are optimal in the sense that they lead to the shortest possible decompression schedules consistent with the assumptions made concerning the relationship between tissue tension and safe depth. However, until any differences in schedules suggested by this method have been carefully tested with real ascents, they cannot be recommended for use in practice.

The practical difficulties involved in executing a complicated schedule approximating the optimal one is recognized. Analogue computer methods^{9,10} are being developed that may eventually automate the controls and make any desired schedule feasible.

The principal value of the continuous ascent schedules at present is to indicate the areas in which improvements over the present schedules may or may not be expected to be possible. The program can also be used to analyze given dive schedules and may be of use in pinpointing the reason if bends result during an actual dive.

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- 4 A E BOYCOTT, G C C DAMANT, AND J S HALDANE, Prevention of compressed air illness, *J Hygiene* 8, 342-443 (1908)
- 5 H BRADNER AND R S MACKAY, Biophysical limitations on deep diving. Some limiting performance expectations, *Bull Math Biophys* 25, 251-72 (1963)
- 6 H R SCHREINER AND P L KELLY, Computation methods for decompression from deep dives, pp. 275-99 in Ref. 1
- 7 G MOELLER, STANDIVE, FORTRAN *Solution of Decompression Equations*, U.S. Naval Submarine Medical Center Report A65, 1966
- 8 The authors are indebted to Arthur Harris, Applied Math Dept., BNL, for suggesting the use of this method for obtaining near-exact approximations in the otherwise intractable equations (19) and (49).
- 9 B A HILLS, A thermal analogue for the optimal decompression of divers Theory, *Phys Med Biol* 12, 437-44 (1967), Construction and use, *Ibid* 445-54
- 10 R A STUBBS AND D J KIDD, Computer analogs for decompression, pp. 300-11 in Ref. 1

APPENDIX A

Principal Variables Used in SIMDIVE and Subroutines, in Order of First Use

Variable	Input format	Explanation
Program SIMDIVE		
LDIVE		Serial number of dive in this run
K	I2	Determines type of run ($K=12$, descent with new parameters, $K=10, 11$, ascent with new parameters, $K=2$, descent with former parameters, $K=0, 1$, ascent with former parameters)
HEAD(7)	7A10	Dive identification
H(9)	9F8 0	Half-times in minutes for nine tissues
AC(9)	9F8 0	Slope of curve relating safe tension to depth
AK(9)	9F8 0	Safe total inert gas partial pressures in tissues, in feet of sea water
DKCON(9)		$\lambda(J) = \log_2 H(J)$
GMIX(4, 10)	2F8 2	Fractional partial pressures of nitrogen and helium for 10 mixtures (total inert = $N_2 + He, O_2 = 1 - total inert$)
FGMIX(3, 10)		Ratio of individual inert gas to total inert gas
T(200)	F8 2	T(1)=starting time, in minutes
DEPTH(200)	F8 2	DEPTH(1)=starting gauge depth in feet of sea water
MAXDEEP	I5	Maximum depth to be shown on graph
RATE	F8 0	Maximum rate of ascent
Q(9, 3)	9F8 4	Total inert, nitrogen, and helium partial pressures (absolute) in nine tissues, in feet of sea water

Variable	Input format	Explanation	Variable	Input format	Explanation		
Subroutine DESCENT							
NEND	A3	Signal for end of descent data	PTI(9)		Provisional time of intersection of J th tissue with critical tissue safe depths		
THOUR	F5 0	Hours component of step time	Subroutine FASTRIZ				
TMIN	F4 2	Minutes component of step time	All variables defined above or by program statements				
DEPTH(200)	F8 0	Gauge depth for step, in feet of sea water	Subroutine PLOT				
KG(200)	I5	Index number identifying gas mix for step	INDEX		Determines ordinate scale		
DTIME(200)		Time interval for step, in minutes	JY(5)		Ordinate labels		
SAFEQ(9)		Safe total inert gas tension, in feet of sea water	ATIME		Time in minutes from $T(1)$ to end of last step		
DD		Change in depth during step, in feet of sea water	TSCALE		Scaling factor for abscissa		
RATE2		Average rate of change of depth for step, in ft/min	POINT(101)		Ordinate location to be plotted		
SAFED(9)		Safe depth (gauge) for total inert gas tension in tissues	IPOINT(50)		POINT's actually used		
Subroutine ASCENT							
STIME		Starting time of ascent, in minutes	NTIME(4)		$NTIME(1), (2)$, beginning step time in HR MIN		
CUTIME		Accumulated ascent time			$NTIME(3), (4)$, end step time in HR MIN		
BLIM		Next depth boundary for change of gas mixture	Subroutine TABLE				
DOD		Absolute external pressure (gauge depth + 33), in feet of sea water	PPRES		Inert gas partial pressure in breathing gas mixture, in feet of sea water, absolute		
DB		Distance from start of step to next BLIM	PRDL		Correction for effect of ascent rate on dQ/dt		
DEVEN		Distance from start of step to next even 10-ft level					

APPENDIX B

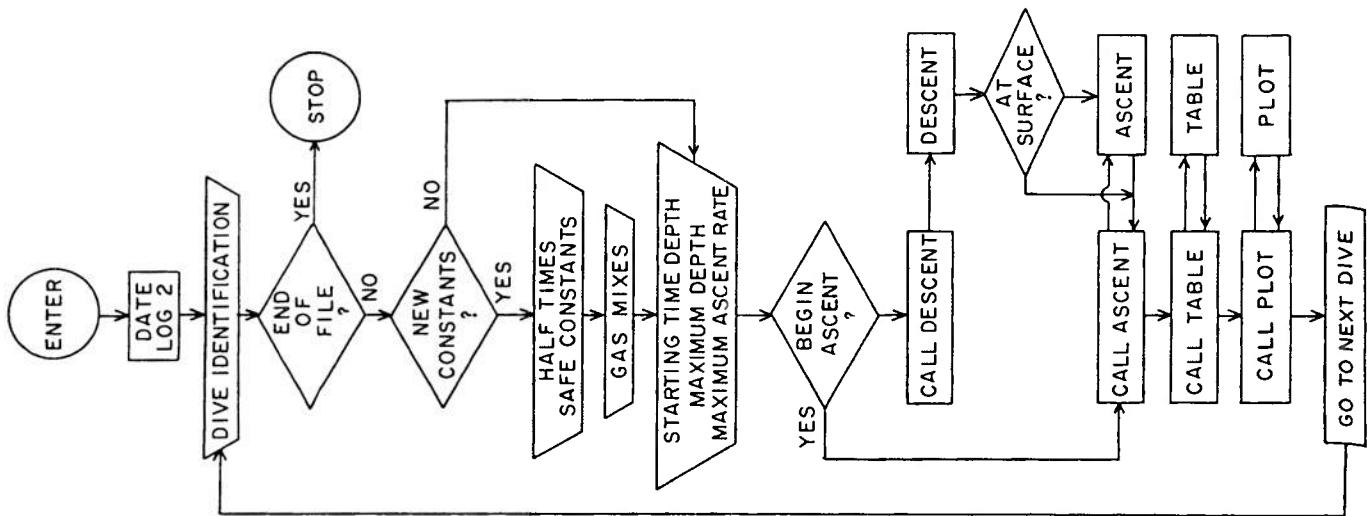
1 Listings and Logic Diagrams for Program SIMDIVE, Subroutine DESCENT, Subroutine ASCENT, Subroutine FASTRIZ, Subroutine PLOT, Subroutine TABLE, and Subroutine TENSION

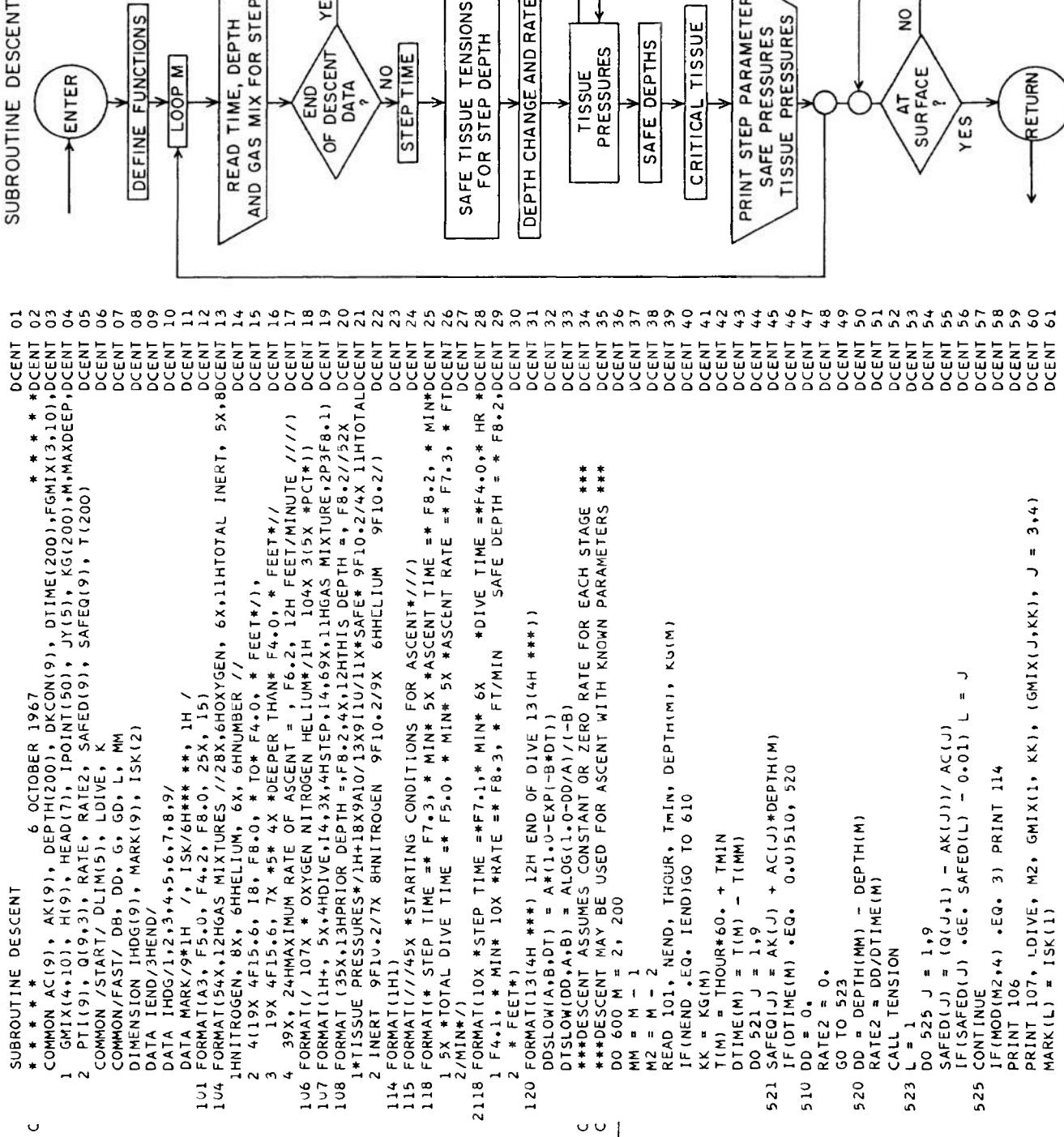
PROGRAM SIMDIVE

```

PROGRAM SIMDIVE(INPUT,OUTPUT,TAPES=INPUT)
* * * * OCTOBER 1967
COMMON AC(9), AK(9), DEPTH(200), DKCON(9), DTIME(200), GMIX(3,10), SDIVE 01
1 GMIX(4,10), H(9), HEAD(7), IPOINT(50), JY(5), KG(200), M,MAXDEEP, SDIVE 02
2 PT1(9), Q(9,3), RATE, RATE2, SAFF(9), SAFEQ(9), T(200) SDIVE 03
COMMON /START/ DLIM(5), LDIVE, K SDIVE 04
DATA DLIM/0.0, 50.0, 100.0, 200.0, 380.0 /
DATA LDIVE/0/
9U FORMAT(12, TA10)
95 FORMAT(1H1 2X 11H DIVE NUMBER 14, 1UX 7A10, 18X A9)
100 FORMAT(16X, 2F8.2, 15, F8.0)
101 FORMAT(8X, 9FB.0)
102 FORMAT(8X, 2F8.2)
104 FORMAT(8X, 9F8.4)
115 FORMAT(4/7 46X *HALF TIMES IN MINUTES FOR NINE TISSUES*/2X *H* 9XSDIVE 10
1 9F12.0/ 53X *TURNOVER RATE CONSTANTS*/2X *LAMBDA* 4X 9F12.6 //) SDIVE 11
116 FORMAT(25X,71H CONSTANTS RELATING SAFE DEPTH TO INERT GAS PARTIAL PSDIVE 12
1IRESSURES IN TISSUES /3H AK,9X,9F12.4/3H AC,9X,9F12.4//) SDIVE 13
C
CALL DATE(DAY)
ECON = ALOG(2.0)
1 LDIVE = LDIVE + 1
READ 90, K, HFAD
IF (EOF,5) 30, ,
5 PRINT 95, LDIVE, HEAD, DAY
IF (K .LT. 10) GO TO 4
READ 101, H, AC, AK
DO 6 J = 1,9
6 DKCON(J) = ECON/H(J)
PRINT 115, H, DKCON
PRINT 116, AK, AC
DO 3 J = 1, 10
3 READ 102, (GMIX(1,J), I=3, 4)
GMIX(2,J) = GMIX(3,J)+GMIX(4,J)
GMIX(1,J) = 1.0-GMIX(2,J)
IF (GMIX(2,J) * GT. 1.E-5) GO TO 35
34 FMIX(1,J) = 0.0
35 DO 3 I = 2, 3
3 FMIX(1,J) = GMIX(I+1,J)/GMIX(2,J)
4 READ 100, T(1), DEPTH(1), MAXDEEP, RATE
IF (MAXDEEP .EQ. 0) MAXDEEP = DEPTH(1)
IF (RATE .EQ. 0.0) RATE = 60.
READ 104, Q
M = 1
IF (MOD(K,10) .LT. 2) GO TO 7
CALL DESCENT
GO TO 8
7 CALL ASCENT
8 PRINT 95, LDIVE, HEAD, DAY
CALL TABLE
PRINT 95, LDIVE, HEAD, DAY
CALL PLOT
CALL TABLE
GO TO 1
30 STOP
END

```



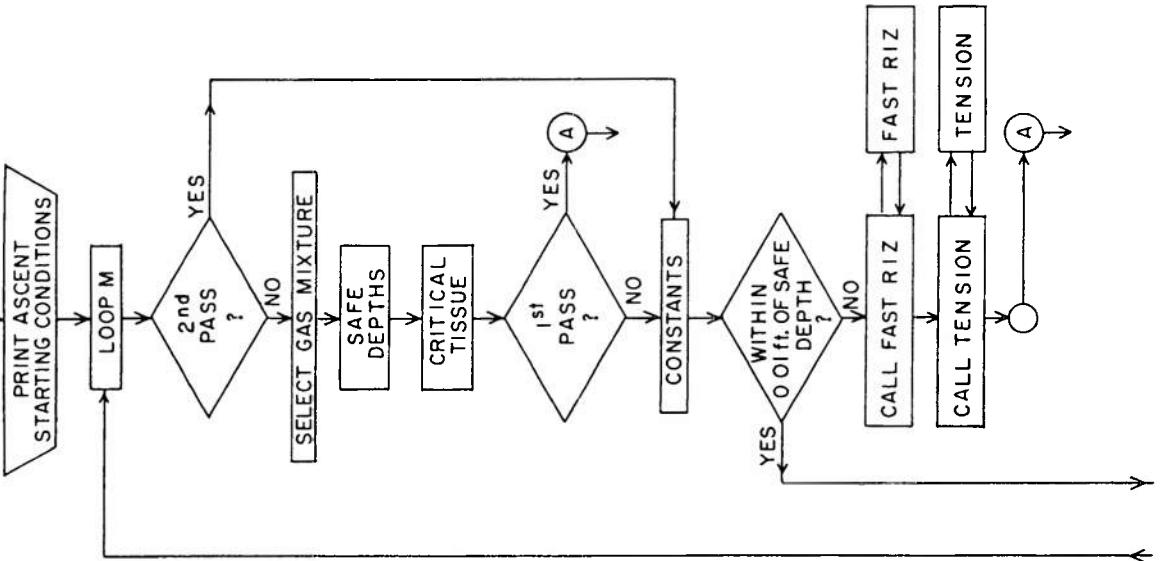


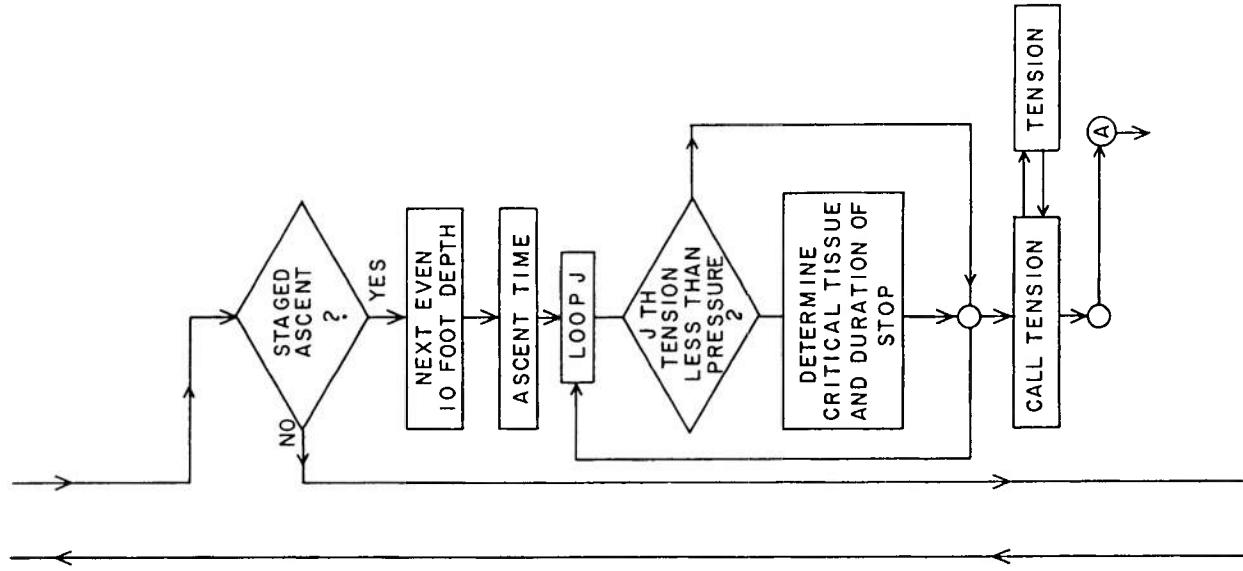
SUBROUTINE ASCENT

```

PRINT 108, ODEPTH(MM), ODEPTH(L), MARK, IHDG, SAFE0, Q
MARK(L) = ISK(2)
PRINT 2118, DTIME(M), THOUR, TMIN, RATE2, SAFE0(L)
600 CONTINUE
610 M = MM
  IF(ODEPTH(M) .LE. 0.0) 20,630
630 PRINT 114
C   *** * * *
C   *** * * * END DESCENT
C   *** * * * BEGIN ASCENT
C   *** * * * COMPUTES CONTINUOUS RATES OF ASCENT. MAINTAINING
C   *** * * * MINIMUM SAFE DEPTH. IT ASSUMES EITHER A MAIN PROGRAM
C   *** * * * GIVING TISSUE PRESSURES AT BOTTOM DEPTH OR PRIOR EXECUTION *
C   * * OF SUBROUTINE DESCENT.
C   ENTRY ASCENT
STIME = T(M)
CUTIME = 0.
RATE2 = 0.
PRINT 115
PRINT 104,((GMIX(I,J),I=1,4), J, DLIM(J+1), OLIM(J), J=1,4),
1 (GMIX(I,5),I = 1,4), DLIM(5), RATE
L = 1
NNN = M + 1
OTIME(NNN) = 0.0
OD = 0.
C
DO 190 M=NNN,200
  MM = M - 1
  M2 = M - 2
  IF(M .EQ. NNN+) 2,3
  GO TO 8
C
  2 KG(M) = KG(MM)
  3 DO 4 KK = 1,4
    IF(ODEPTH(MM) .GT. OLIM(KK+1)) 4,5
    4 CONTINUE
    KK = 5
    5 BLIM = DLIM(KK)
    KG(M) = KK
    C
    ODEPTH(M) = (O(L,1)-AK(L))/AC(L)
    O(L,1) = 1.9
    SAFE0(J) = (O(J,1)-AK(J))/AC(J)
    IF(SAFE0(J) .GE. SAFE0(LL) - .01) L = J
    7 CONTINUE
    LL = L
    IF(M .EQ. NNN)GO TO 180
    D00 = ODEPTH(M) + 33.
    G = GMIX(2,KK)
    GD = G * D0D
    DB = DEPTH(MM) - BLIM
    DEVEN = AMOD(DEPTH(MM), 10.)
    IF(OEVEN .LT. 0.01)DEVEN = OEVEN + 10.
    DD = DEPTH(MM) - SAFE0(L)
    IF(DD .LT. 0.01) GO TO 292 FAST ASCENT
    CALL FASTRIZ
    CALL TENSION
    GO TO 180
    IF(MOO(K,10) .LT. 3) GO TO 295
  180
  190
C
  292

```





* * * * * OPTION FOR STAGED ASCENT

```

C 293 DD = 0.
      RATE2 = 0.
      DNEXT = DEPTH(MM) - DEVEN
      DFT = DEVEN.RATE
      DTIME(M) = 1.0
DO 294 J = L, 9
      IF(Q(J,1) * LE. GD) GO TO 294
      QNEXT = AK(J) + DNEXT * AC(J)
      GRD = G * RATE/DKCON(J)
      DKT = DKCON(J) * DFT
      GSL = GRD + (QNEXT - GD + GRD*(DKT-1.))*EXP(DKT)
      TNEXT = ALOG((Q(J,1) - GD)/QSL)/DKCON(J)
      IF(TNEXT .LT. DTIME(M)) GO TO 294
      DTIME(M) = TNEXT
      LL = J
CONTINUE
      IF(DTIME(M) .GT. 300.) DTIME(M) = 300.
      CALL TENSION
      GO TO 180
294

```

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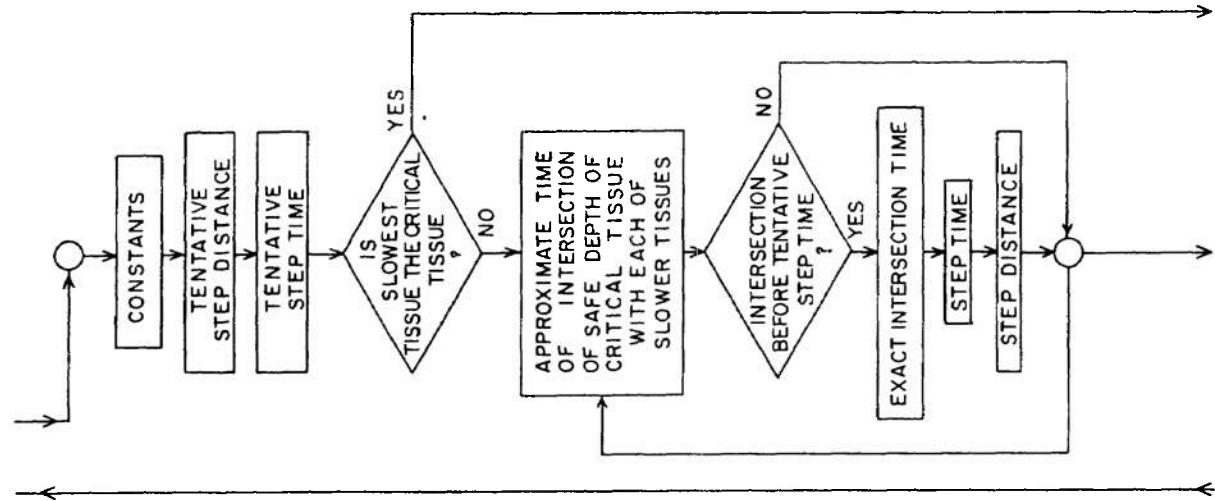
C 295 CONONE = 1. / (AC(L) - G)
DKL = DKCON(L) / AC(L)
CONL1 = DKL * (AC(L) - G)
QGL = Q(L,1) - GD
CON4 = QGL * CONONE
CON2 = CON4 * G
CON3 = GD - CON2
DO = AMIN1(DB, AMAX1(DD, CON4, CONL1))
DTIME = DTslow(DD, CON4, CONL1)
TEST FOR CROSSOVER TO NEW CRITICAL TISSUE
IF (L .EQ. 9) GO TO 315
RATE4 = QGL*DKL
LJ = L + 1
DO 313 J = LJ, 9
DKJ = DKCON(J) / AC(J)
Z1 = DEPTH(MM) - SAFED(J)
PT1 = Z1 / (RATE4 - (O(J,1) - GD) * DKL)
IF (PT1 .GE. DTIME) GO TO 311
LL = J
Z1 = Z1 * AC(J)
Z3 = O(J,1) - CON3
Z4 = CON2 * DKCON(J)
Z5 = CON4*AC(J)
TEST = DKCON(J) - CONL1
IF (ABS(TEST) .GT. 1.0E-6) GO TO 309
DO 308 KM = 1.5
EXP2 = EXP(-DKCON(J)*PT1)
PT1 = PT1 - ((Z5-Z3)-(Z5-Z4)*PT1)*EXP2-Z1)/((CONL1*(Z5-Z3)) +
1.24*(1.-CONL1*PT1))*EXP2
GO TO 311
309 Z4 = 24/TEST
DO 310 KM = 1.5
EXP1 = EXP(-CONL1*PT1)
EXP2 = EXP(-DKCON(J)*PT1)
310 PT1 = PT1 + (Z5-Z3+(Z4-Z2)*EXP1+(Z3-Z4)*EXP2-Z1)/(CONL1*(Z4-Z5))*EXP1
1. + DKCON(J) * (Z3-Z4)*EXP2
311 DTIME = AMIN1(DTIME, PT1)
DD = DTslow(CON4, CONL1, DTIME)
313 CONTINUE COMPUTE INERT GAS PRESSURES IN TISSUES
C 315 DO 98 J = 1, 9
EXPO = DKCON(J)*DTIME
EXP2 = EXP(-EXPO)
TEST = DKCON(J) - CONL1
IF (ABS(TEST) .GT. 1.0E-6) GO TO 319
CON8 = EXP0 * CON2
Q(J,1) = CON3 + (Q(J,1) - CON3 + CON8) * EXP2
DO 318 I = 2,3
CON9 = FGmix(I,KK) * CON3
Q(J,1) = CON9 + (Q(J,1)-CON9+FGmix(I,KK)*CON8)*EXP2
318 Q(J,1) = CON9 + (Q(J,1)-CON9+FGmix(I,KK)*CON8)*EXP2
GO TO 98
319 CON5 = DKCON(J) * CON2 / TEST
CON6 = CON3 + CON5*EXP(-CONL1*DTIME)
CON7 = CON3 + CON5
Q(J,1) = CON3 + (Q(J,1) - CON7)*EXP2
DO 98 I = 2,3
Q(J,1) = FGmix(I,KK)*CON6 + (Q(J,1)-FGmix(I,KK)*CON7)*EXP2
98 CONTINUE
RATE2 = DD/DTIME
DTIME(M) = DTIME

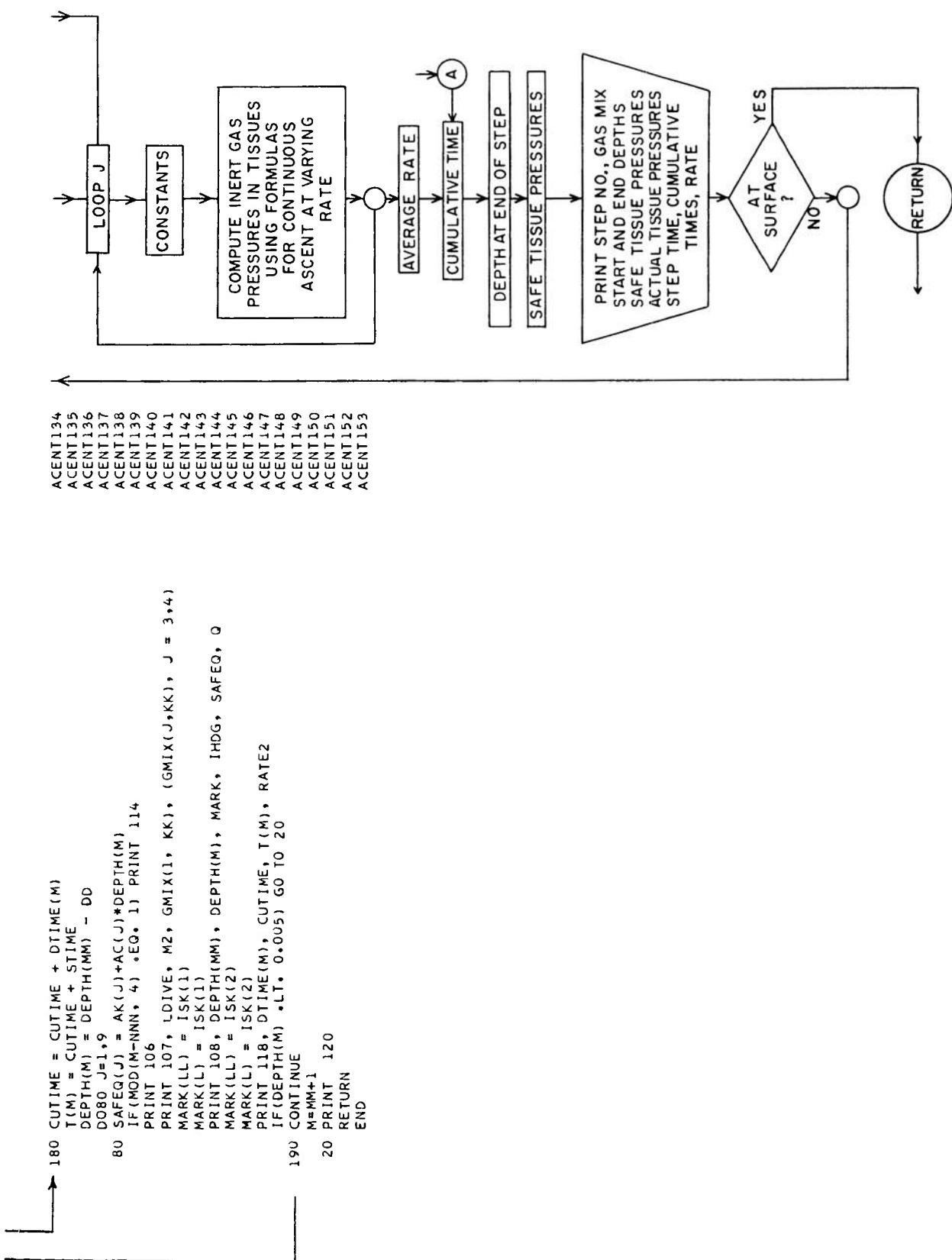
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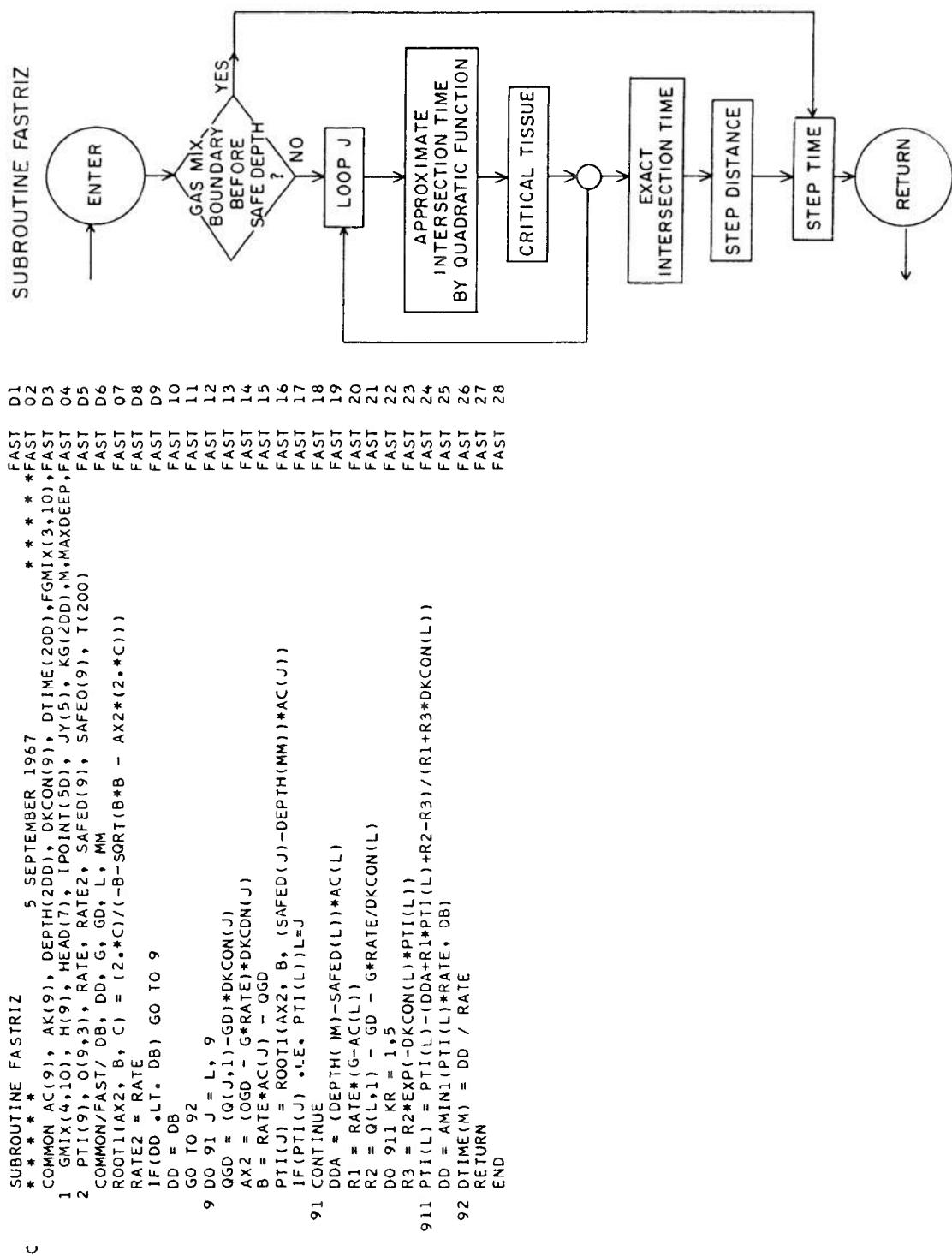
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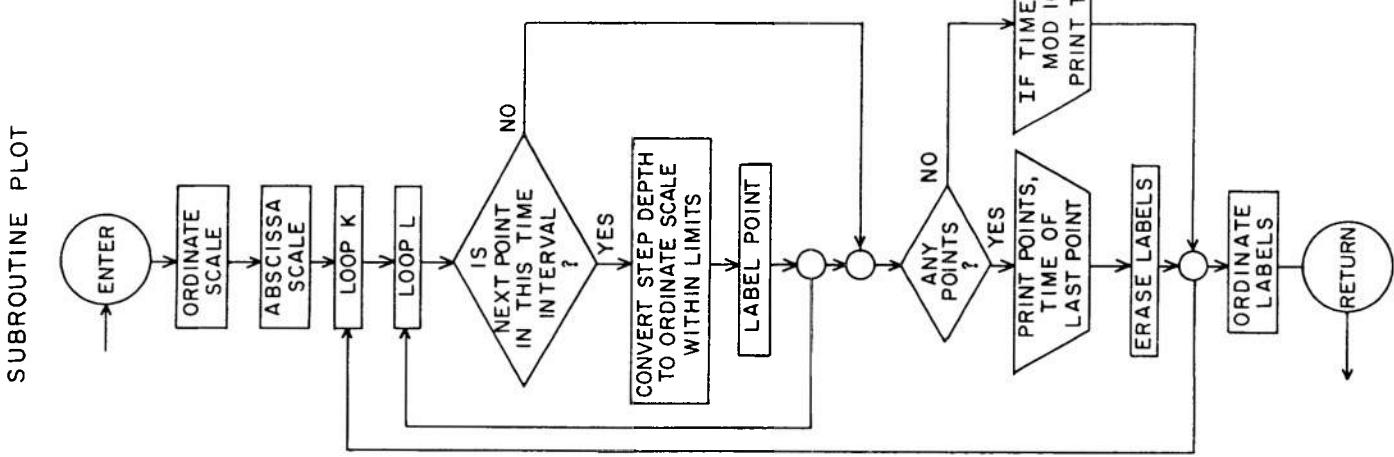


SUBROUTINE PLOT

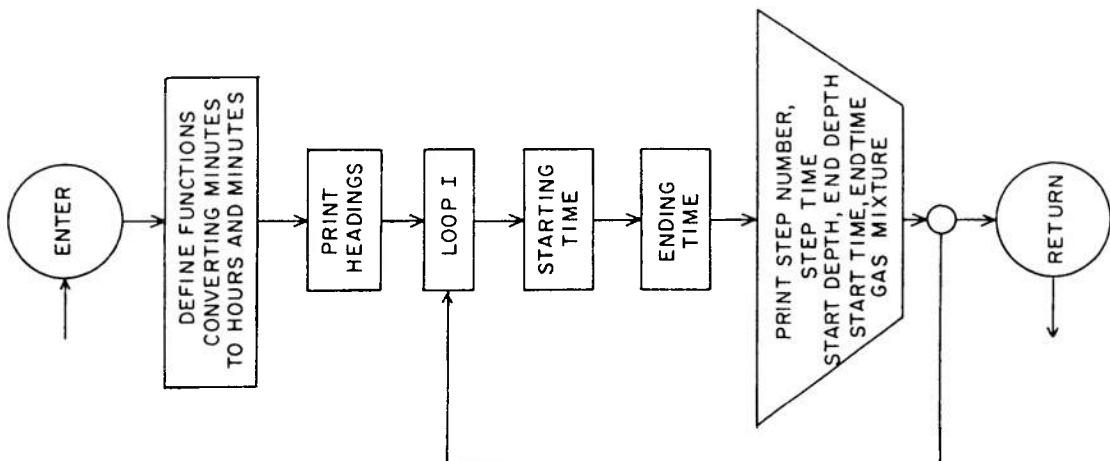
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C * * * * * 15 AUGUST 1967 * * * * *
COMMON AC(9), AK(9), DEPTH(200), DKCON(9), DTIME(200), FGMIX(3,10), PLOT
1 GMIX(4,10), H(9), HEAD(7), IPOINT(50), JY15(), KG(200,M,MAXDEEP), PLOT
2 PTI(9), Q(9,3), RATE, RATE2, SAFFED(9), SAFEQ(9), T(200) PLOT
COMMON /KPLOT/ POINT(101), SCALE(5), SLIM(4), TAB(2) PLOT
DATA POINT/101(1H) /
DATA SCALE/1.0 0.2 0.5 0.10 0.20 0. /
SLIM/120. 240. 600. 1200. /
DATA TAB/1H*, 1H /
FORMAT(1H+, 13X, 103(1H-)/15X,1H1,4(24X,1H1))
1005 FORMAT(5X,7.2,2H 1,101A1,1H1)
1007 FORMAT(6X, 14, 4X 1H1, 101X, 1H1)
1008 FORMAT(13X,2H 1,101X,1H1)
1023 FORMAT(1/8H TIME, 50X, 13HDEPTH IN FEET / 11H IN MINUTES )
1024 FORMAT(14X,13,3(22X,13),23X11)
1100 FORMAT(58X, 13HDEPTH IN FEET )
IF(DEPTH(M) .LT. 0.0) DEPTH(M)=0.0
INDEX = (MAXDEEP + 99)/100
DO 2 I = 1,*5
2 JY(I) = INDEX*25*(5-1)
PRINT 1023
PRINT 1024,JY
PRINT 1003
ATIME T(M) - T(1)
DO 3 IS = 1,4
IF(ATIME .LE. SLIM(IS))4, 3
3 CONTINUE
IS = 5
4 TSCALE = 1.0/SCALE(IS)
KMAX = INT(ATIME*TSCALE+1.5)
ISCALE = INT(TSCALE*IS)
N=1
DO 9 K = 1, KMAX
KL = K-1
KF = 1
KP = 0
DO 37 L=N,M
IF(INT(T(L) - T(1))*TSCALE+0.5) .GT. KL ) GO TO 38
N=L
1 = MAX0(1, MIN0(101-INT(DEPTH(L)+0.5)/INDEX, 101))
POINT(1) = TA8(1)
IPOINT(KP) = 1
KF = 2
CONTINUE
38 GO TO (6,5),KF
5 PRINT 1005,(N),POINT
DO 51 L = 1, KP
1=IPOINT(L)
POINT(1) = TA8(2)
N = N + 1
GO TO 9
6 KLS = KL*TSCALE + INT(T(1) + .5)
IF(MOD(KLS, 10) .NE. 0) GO TO 8
PRINT 1007,KLS
GO TO 9
8 PRINT 1008
9 CONTINUE
PRINT 1003
PRINT 1024, JY
PRINT 1100
RETURN
END

```



SUBROUTINE TABLE

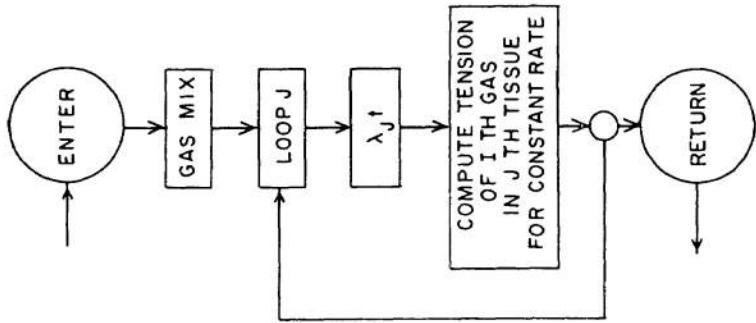


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* * * * *          15 AUGUST 1967          * * * * *          TABLE 01
C      COMMON AC(9), AK(9), DEPTH(200), OKCON(9), DTIME(200), FG MIX(3,10), TABLE 02
1      GMIX(4,10), H(9), HEAO(7), IPOINT(50), JY(5), KG(200), M, MAXOEEP, TABLE 03
2      PT(9), Q(9,3), RATE, RATE2, SAFED(9), SAFEQ(9), T(200)   TABLE 04
DIMENSION NTI(IE(4))   TABLE 05
T(200)   TABLE 06
1002 FORMAT(//3X *STEP* 3X *STEP TIME* 6X*DEPTH* 10X *CUMULATIVE TIME*TABLE 07
1* 10X *OXYGEN NITROGEN HELIUM*/13X *MIN* 10X *FEET* 11X *H M* 5X TABLE 08
2 *H M* 8X 3(5X *PCT*) /)   TABLE 09
1003 FORMAT(1H 15,2F10.0,*-* F4.0,110,*9*12,*-* 14,*9*12, 8X2P 3F8.1) TABLE 10
NHR(IMIN) = IMIN/60   TABLE 11
NMN(IMIN) = MOOLIMN,60   TABLE 12
NTIME(3)=NHR(INT(T(1)))   TABLE 13
NTIME(4)=NMN(INT(T(1)))   TABLE 14
PRINT 1002   TABLE 15
00 100 1=2,M   TABLE 16
11=I-1   TABLE 17
M2 = 1 - 2   TABLE 18
KK = KG(I)   TABLE 19
NTIME(1)=NTIME(3)   TABLE 20
NTIME(2)=NTIME(4)   TABLE 21
INTT=INTT(I)   TABLE 22
NTIME(3)=NHR(INTT)
NTIME(4)=NMN(INTT)   TABLE 23
PRINT 1003, M2, NTIME(I), DEPTH(I), NTIME, GMIX(1,KK), TABLE 24
1 (GMIX(J,KK), J=3,4)   TABLE 25
100 CONTINUE   TABLE 26
RETURN   TABLE 27
END   TABLE 28
TABLE 29

```

SUBROUTINE TENSION



```

C      * * * * *          15 AUGUST 1967          * * * * *
COMMON AC(9), AK(9), DEPTH(20D), DKCON(9), DTIME(200), FG MIX(3,10), *TENSN 01
1   GMIX(4,10), H(9), HEAD(7), IPOINT(50), JY(5), KG(200), M, MAXDEEP, TENSN 02
2   PT(9), Q(9,3), RATE, RATE2, SAFFED(9), SAFEQ(9), T(2D0)          TENSN 03
QPRESS(A,B,C,D) = A-B*(C-1.) + (D-A-B)*EXP(-C)          TENSN 04
KK = KG(M)          TENSN 05
DD 19 J 1,9          TENSN 06
EFACT = DKCON(J)*DTIME(M)          TENSN 07
RDK = RATE2/DKCON(J)          TENSN 08
DD 18 I=3,4          TENSN 09
PPRES = GMIX(1,KK)*(DEPTH(M-1) + 33.0)          TENSN 10
PRDL = GMIX(1,KK) * RDK          TENSN 11
18 Q(J,I-1) = QPRES*PPRES, PRDL, EFACT, Q(J,I-1)          TENSN 12
19 Q(J,1) = Q(J,2) + Q(J,3)          TENSN 13
RETURN          TENSN 14
END          TENSN 15
          TENSN 16
          TENSN 17

```

COMPUTE TENSION
OF I TH GAS
IN J TH TISSUE
FOR CONSTANT RATE

2. Data Deck for the 450-Foot, 60-Minute Dive Presented in Appendix C

SAMPLE DATA DECK

APPENDIX C

Computer Output for 450-Foot, 60-Minute Dive, With Ascent by the Continuous Method

The first 6 steps are produced by the DESCENT subroutine. The 7th step indicates the diver's tissue inert gas partial pressure status at the beginning of ascent. During the fast rise there is a "stop" at 380 ft because this is entered as a gas mixture boundary. (Actually in this dive the gas mixture does not change, and the stop is unnecessary.) From the 10th step to the time of surfacing on the 42nd step ASCENT uses the continuous ascent method, with the ascent rate governed by the rate of change of the safe depth. The rate printed out for each step is the mean ascent rate for that step.

DIVE NUMBER 1

*** DIVE TO 450 FEET FOR 60 MINUTES. CONTINUOUS ASCENT ***

03/01/68

H	5	10	HALF TIMES IN MINUTES FOR NINE TISSUES
			20 40 80 120
LAMBDA	,138629	,069315	TURNOVER RATE CONSTANTS
			,017329 ,008664
AK	86,0000	CONSTANTS RELATING SAFE DEPTH TO INERT GAS PARTIAL PRESSURES IN TISSUES	
	74,0000	66,0000 60,0000 56,0000 54,0000	
AC	1,5000	1,4000 1,3000 1,2000 1,2000	
		53,0000 53,0000	
		1,0000 1,0000	

DIVE	1	STEP	0	PRIOR DEPTH =	0.00	THIS DEPTH =	0.00	GAS MIXTURE	OXYGEN NITROGEN HELIUM
				TISSUE PRESSURES	4	5	**6**		PCT
SAFE	86.00	74.00	66.00	60.00	56.00	54.00	53.00	53.00	0.0
TOTAL INERT	26.08	26.08	26.08	26.08	26.08	26.08	26.08	26.08	26.08
- NITROGEN	26.08	26.08	26.08	26.08	26.08	26.08	26.08	26.08	26.08
HELIUM	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
STEP TIME =	0.0 MIN	DIVE TIME =	0 HR	0.0 MIN	RATE =	0.000 FT/MIN	SAFE DEPTH =	*23.27 FEET	
DIVE	1	STEP	1	PRIOR DEPTH =	0.00	THIS DEPTH =	75.00	GAS MIXTURE	OXYGEN NITROGEN HELIUM
				TISSUE PRESSURES	4	5	**6**		PCT
SAFE	198.50	179.2	163.50	150.00	146.00	144.00	136.50	128.00	128.00
TOTAL INERT	30.00	28.08	27.09	26.59	26.33	26.25	26.20	26.18	26.16
- NITROGEN	30.00	28.06	27.09	26.59	26.33	26.25	26.20	26.18	26.16
HELIUM	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
STEP TIME =	1.0 MIN	DIVE TIME =	0 HR	1.0 MIN	RATE =	*75.000 FT/MIN	SAFE DEPTH =	*23.13 FEET	
DIVE	1	STEP	2	PRIOR DEPTH =	75.00	THIS DEPTH =	150.00	GAS MIXTURE	OXYGEN NITROGEN HELIUM
				TISSUE PRESSURES	4	5	**6**		PCT
SAFE	311.00	284.2	261.00	240.00	234.00	219.00	203.00	203.00	96.0
TOTAL INERT	44.31	35.58	30.93	28.53	27.31	26.90	26.57	26.49	
- NITROGEN	26.12	26.20	26.17	26.13	26.10	26.10	26.09	26.09	
HELIUM	18.19	9.38	4.77	2.40	1.21	.80	.60	.48	.40
STEP TIME =	1.0 MIN	DIVE TIME =	0 HR	2.0 MIN	RATE =	*75.000 FT/MIN	SAFE DEPTH =	*22.58 FEET	

OXYGEN NITROGEN HELIUM
PCT PCT PCT
4.0 0.0 96.0

DIVE 1 STEP 3 PRIOR DEPTH = 150.00 THIS DEPTH = 250.00 GAS MIXTURE

TISSUE PRESSURES			
	4	5	6
SAFE	461.00	424.00	391.00
INERT	67.67	48.22	37.51
NITROGEN	22.74	24.45	25.28
HELIUM	44.93	23.77	12.23

STEP TIME = 1.0 MIN DIVE TIME = 0 HR 3.0 MIN RATE = -100.000 FT/MIN SAFE DEPTH = -12,22 FEET

OXYGEN NITROGEN HELIUM
PCT PCT PCT
4.0 0.0 96.0

DIVE 1 STEP 4 PRIOR DEPTH = 250.00 THIS DEPTH = 350.00 GAS MIXTURE

TISSUE PRESSURES			
	4	5	6
SAFE	611.00	564.00	521.00
INERT	100.44	66.43	47.13
NITROGEN	19.79	22.81	24.42
HELIUM	60.64	43.62	22.71

STEP TIME = 1.0 MIN DIVE TIME = 0 HR 4.0 MIN RATE = -100.000 FT/MIN SAFE DEPTH = 9,62 FEET

OXYGEN NITROGEN HELIUM
PCT PCT PCT
4.0 0.0 96.0

DIVE 1 STEP 5 PRIOR DEPTH = 350.00 THIS DEPTH = 450.00 GAS MIXTURE

TISSUE PRESSURES			
	4	5	6
SAFE	761.00	704.00	651.00
INERT	141.39	89.86	59.69
NITROGEN	17.23	21.28	23.58
HELIUM	124.16	68.58	36.11

STEP TIME = 1.0 MIN DIVE TIME = 0 HR 5.0 MIN RATE = -100.000 FT/MIN SAFE DEPTH = 36,92 FEET

OXYGEN NITROGEN HELIUM
PCT PCT PCT
4.0 0.0 96.0

DIVE 1 STEP 6 PRIOR DEPTH = 450.00 THIS DEPTH = 450.00 GAS MIXTURE

TISSUE PRESSURES			
	4	5	6
SAFE	761.00	704.00	651.00
INERT	463.52	455.42	405.63
NITROGEN	463.01	454.47	3.51
HELIUM	463.51	454.95	400.12

STEP TIME = 5.0 MIN DIVE TIME = 1 HR 0.0 MIN RATE = 0.000 FT/MIN SAFE DEPTH = 272,44 FEET

STARTING CONDITIONS FOR ASCENT

GAS MIXTURES				NUMBER
OXYGEN	TOTAL INERT	NITROGEN	HELIUM	
.209020	.790180	.790180	0.000000	1
.209020	.790180	.790180	0.000000	2
.209020	.790180	.790180	0.000000	3
.040000	.960000	0.000000	.960000	4
.040000	.960000	0.000000	.960000	5

DEEPR THAN 180 FEET

MAXIMUM RATE OF ASCENT = 60.00 FEET/MINUTE

DIVE	1	STEP	7	PRIOR DEPTH =	450.00	THIS DEPTH =	450.00	GAS MIXTURE	OXYGEN	NITROGEN	HELIUM
									PCT	PCT	PCT
SAFE	1	***2*	*	3	4	5	6	7	8	9	
TOTAL INERT	761.00	704.00	651.00	600.00	596.00	594.00	549.00	503.00	503.00		
TOTAL NITROGEN	463.52	455.42	403.63	301.62	197.39	149.45	122.32	104.94	92.86		
TOTAL HELIUM	.01	.04	.51	.56	.79	.67	.29	.34	.22	.16	
ASCENT TIME =	0.000 MIN	ASCENT TIME =	0.00 MIN	TOTAL DIVE TIME =	60 MIN			ASCENT RATE =	0.000 FT/MIN		

DIVE 1 STEP 8		PRIOR DEPTH = 450.00	THIS DEPTH = 380.00	GAS MIXTURE		
		Tissue Pressures			OXYGEN	NITROGEN
		4	5	6	HELIUM	PCT
SAFE	656.00	560.00	516.00	510.00	472.00	433.00
TOTAL INERT	458.39	404.67	304.19	199.73	151.33	106.25
NITROGEN	.01	3.37	9.37	15.63	18.54	21.25
HELIUM	458.39	401.30	294.81	184.10	132.79	85.00
STEP TIME =	1.167 MIN	ASCENT TIME =	1.17 MIN	TOTAL DIVE TIME =	61 MIN	ASCENT RATE = 60,000 FT/MIN
DIVE 1 STEP 9		PRIOR DEPTH = 380.00	THIS DEPTH = 260.34	GAS MIXTURE		
		Tissue Pressures			OXYGEN	NITROGEN
		4	5	6	HELIUM	PCT
SAFE	476.51	404.45	372.41	368.41	366.41	340.38
TOTAL INERT	428.93	400.24	305.36	202.12	153.48	125.73
NITROGEN	.01	3.38	3.14	9.05	15.37	20.02
HELIUM	428.92	436.10	397.10	296.31	186.75	105.71
STEP TIME =	1.994 MIN	ASCENT TIME =	3.16 MIN	TOTAL DIVE TIME =	63 MIN	ASCENT RATE = 60,000 FT/MIN
DIVE 1 STEP 10		PRIOR DEPTH = 260.34	THIS DEPTH = 254.82	GAS MIXTURE		
		Tissue Pressures			OXYGEN	NITROGEN
		4	5	6	HELIUM	PCT
SAFE	468.23	430.74	397.26	365.78	361.78	359.78
TOTAL INERT	414.73	430.74	397.26	305.03	202.59	154.00
NITROGEN	.00	3.36	5.06	8.94	15.27	18.25
HELIUM	414.73	430.39	394.20	296.09	187.32	135.74
STEP TIME =	0.717 MIN	ASCENT TIME =	3.88 MIN	TOTAL DIVE TIME =	64 MIN	ASCENT RATE = 7,706 FT/MIN
DIVE 1 STFP 11		PRIOR DEPTH = 254.82	THIS DEPTH = 250.00	GAS MIXTURE		
		Tissue Pressures			OXYGEN	NITROGEN
		4	5	6	HELIUM	PCT
SAFE	461.00	424.00	391.00	360.00	356.00	354.00
TOTAL INERT	388.23	415.22	391.00	304.23	203.52	155.04
NITROGEN	.00	3.32	2.91	8.71	15.07	18.10
HELIUM	388.22	414.90	388.09	295.52	188.44	136.94
STEP TIME =	1.504 MIN	ASCENT TIME =	5.36 MIN	TOTAL DIVE TIME =	65 MIN	ASCENT RATE = 7,706 FT/MIN

DIVE 1 STEP 12		PRIOR DEPTH = 250.00	THIS DEPTH = 240.00	GAS MIXTURE			OXYGEN PCT 4.0	NITROGEN PCT 0.0	HELIOUM PCT 96.0
SAFE	446.00 ¹	410.00 ²	***3**	4	5	6	7	8	9
TOTAL INERT	344.73	385.76	378.00	348.00	344.00	342.00	318.00	293.00	293.00
NITROGEN	.00	.26	.00	.22	.24	.24	.08	.87	.11
HELIUM	344.73	385.50	2.60	8.24	14.66	17.77	19.55	20.71	21.52
STEP TIME = 3,189 MIN	ASCENT TIME = 8.57 MIN	TOTAL DIVE TIME = 69 MIN	ASCENT RATE = 3.135 FT/MIN						
DIVE 1 STEP 13		PRIOR DEPTH = 240.00	THIS DEPTH = 230.00	GAS MIXTURE			OXYGEN PCT 4.0	NITROGEN PCT 0.0	HELIOUM PCT 96.0
SAFE	431.00 ¹	396.00 ²	***3**	4	5	6	7	8	9
TOTAL INERT	312.61	359.56	365.00	336.00	332.00	330.00	307.00	283.00	283.00
NITROGEN	.00	.21	.00	.73	.70	.70	.89	112.53	99.42
HELIUM	312.60	359.35	2.32	7.79	14.25	17.43	19.28	20.48	21.32
STEP TIME = 3,284 MIN	ASCENT TIME = 11.86 MIN	TOTAL DIVE TIME = 72 MIN	ASCENT RATE = 3.045 FT/MIN						
DIVE 1 STEP 14		PRIOR DEPTH = 230.00	THIS DEPTH = 220.00	GAS MIXTURE			OXYGEN PCT 4.0	NITROGEN PCT 0.0	HELIOUM PCT 96.0
SAFE	416.00 ¹	382.00 ²	***3**	4	5	6	7	8	9
TOTAL INERT	288.14	336.12	352.00	324.00	320.00	318.00	296.00	273.00	273.00
NITROGEN	.00	.16	.00	.76	.76	.88	.68	132.59	114.11
HELIUM	288.14	335.95	2.07	7.34	13.84	17.09	19.00	20.24	21.11
STEP TIME = 3,385 MIN	ASCENT TIME = 15.24 MIN	TOTAL DIVE TIME = 75 MIN	ASCENT RATE = 2.954 FT/MIN						
DIVE 1 STEP 15		PRIOR DEPTH = 220.00	THIS DEPTH = 210.00	GAS MIXTURE			OXYGEN PCT 4.0	NITROGEN PCT 0.0	HELIOUM PCT 96.0
SAFE	401.00 ¹	368.00 ²	***3**	4	5	6	7	8	9
TOTAL INERT	268.77	314.99	339.00	312.00	308.00	306.00	285.00	263.00	263.00
NITROGEN	.00	.13	1.83	2.93	3.31	2.78	2.22	134.17	115.60
HELIUM	268.77	314.86	337.17	286.40	195.36	145.47	115.46	95.60	81.53
STEP TIME = 3,492 MIN	ASCENT TIME = 18.73 MIN	TOTAL DIVE TIME = 79 MIN	ASCENT RATE = 2.864 FT/MIN						

DIVE 1 STEP 16				PRIOR DEPTH = 210.00	THIS DEPTH = 200.00	GAS MIXTURE	OXYGEN PCT 4.0	NITROGEN PCT 96.0	HELIUM PCT 0.0
SAFE	366.00	354.00	**3**	326.00	300.00	294.00	274.00	253.00	9
TOTAL INERT	252.75	295.81		326.00	289.38	209.39	163.59	117.00	103.74
NITROGEN	0.00	10		1.62	6.49	13.01	16.41	18.42	20.68
HELIUM	252.75	295.71		324.38	282.89	196.37	147.18	117.21	83.05
STEP TIME = 3.606 MIN	ASCENT TIME = 22.34 MIN			TOTAL DIVE TIME = 82 MIN			ASCENT RATE = 2.773 FT/MIN		
DIVE 1 STEP 17				PRIOR DEPTH = 200.00	THIS DEPTH = 190.00	GAS MIXTURE	OXYGEN PCT 21.0	NITROGEN PCT 79.0	HELIUM PCT 0.0
SAFE	371.00	340.00	**3**	313.00	288.00	284.00	262.00	243.00	9
TOTAL INERT	230.06	276.10		313.00	284.40	208.71	163.84	136.15	117.59
NITROGEN	56.04	30.73		17.51	14.41	16.87	18.93	20.30	21.24
HELIUM	174.02	245.37		295.49	269.99	191.85	144.91	115.85	96.75
STEP TIME = 2.692 MIN	ASCENT TIME = 25.03 MIN			TOTAL DIVE TIME = 85 MIN			ASCENT RATE = 3.714 FT/MIN		
DIVE 1 STEP 18				PRIOR DEPTH = 190.00	THIS DEPTH = 184.68	GAS MIXTURE	OXYGEN PCT 21.0	NITROGEN PCT 79.0	HELIUM PCT 0.0
SAFE	363.03	332.56	**3**	306.09	281.62	277.62	275.62	257.15	8
TOTAL INERT	219.71	266.20		306.09	281.62	208.27	163.93	136.39	117.87
NITROGEN	77.82	44.64		25.30	18.43	18.86	20.25	21.28	104.63
HELIUM	141.89	221.56		280.78	263.19	169.41	143.68	115.11	95.86
STEP TIME = 1.473 MIN	ASCENT TIME = 26.50 MIN			TOTAL DIVE TIME = 87 MIN			ASCENT RATE = 3.611 FT/MIN		
DIVE 1 STEP 19				PRIOR DEPTH = 184.68	THIS DEPTH = 180.00	GAS MIXTURE	OXYGEN PCT 21.0	NITROGEN PCT 79.0	HELIUM PCT 0.0
SAFE	356.00	326.00	**4**	300.00	276.00	272.00	270.00	252.00	8
TOTAL INERT	202.87	248.23		292.73	276.00	207.30	164.03	136.82	118.41
NITROGEN	109.07	68.08		39.54	26.08	22.72	22.01	23.19	23.54
HELIUM	93.80	180.15		253.19	249.92	184.58	141.22	113.64	94.87
STEP TIME = 2.985 MIN	ASCENT TIME = 29.49 MIN			TOTAL DIVE TIME = 89 MIN			ASCENT RATE = 1.569 FT/MIN		

		OXYGEN NITROGEN HELIUM			
DIVE	STEP	PRIOR DEPTH =	THIS DEPTH =	GAS MIXTURE	
		180.00	170.00	21.0	79.0
TISSUE PRESSURES					
SAFE	1	341.00	312.00	287.00	264.00
TOTAL INERT	179.51	217.48	266.60	264.00	264.00
NITROGEN	141.71	103.52	64.67	40.92	30.54
HELIUM	37.80	114.36	204.75	223.08	174.38
STEP TIME =	6.556 MIN	ASCENT TIME =	36.05 MIN	TOTAL DIVE TIME =	96 MIN
OXYGEN NITROGEN HELIUM					
				21.0	79.0
TISSUE PRESSURES					
SAFE	1	298.00	274.00	252.00	248.00
TOTAL INERT	165.02	194.37	243.37	252.00	202.14
NITROGEN	150.34	123.09	84.11	53.79	37.76
HELIUM	14.69	71.28	159.26	198.21	164.38
STEP TIME =	6.821 MIN	ASCENT TIME =	42.87 MIN	TOTAL DIVE TIME =	103 MIN
OXYGEN NITROGEN HELIUM					
				21.0	79.0
TISSUE PRESSURES					
SAFE	1	284.00	261.00	236.00	234.00
TOTAL INERT	154.28	176.41	222.63	240.00	198.94
NITROGEN	148.80	152.86	98.14	64.75	44.37
HELIUM	5.48	43.55	124.49	175.25	154.56
STEP TIME =	7.107 MIN	ASCENT TIME =	49.97 MIN	TOTAL DIVE TIME =	110 MIN
OXYGEN NITROGEN HELIUM					
				21.0	79.0
TISSUE PRESSURES					
SAFE	1	270.00	248.00	228.00	224.00
TOTAL INERT	145.08	161.89	204.00	228.00	195.30
NITROGEN	143.12	135.84	107.74	73.90	50.37
HELIUM	1.96	26.04	96.26	154.10	144.94
STEP TIME =	7.420 MIN	ASCENT TIME =	57.39 MIN	TOTAL DIVE TIME =	117 MIN
OXYGEN NITROGEN HELIUM					
				21.0	79.0
ASCENT RATE = 1.525 FT/MIN					
ASCENT RATE = 1.466 FT/MIN					
ASCENT RATE = 1.407 FT/MIN					

DIVE 1 STEP 24 PRIOR DEPTH = 140.00 THIS DEPTH = 130.00 GAS MIXTURE
 21.0 PCT
 79.0 PCT
 0.0 PCT

	SAFE	281.00	2	256.00	3	235.00	4	216.00	5	212.00	6	210.00	7	197.00	8	183.00	9	
TOTAL INERT	136.48			149.60		187.15		216.00		193.23		160.90		138.33		121.79		109.33
NITROGEN	135.81			134.40		113.59		81.29		55.72		45.96		40.96		37.95		35.94
HELIUM	.67			15.21		73.56		134.71		135.51		114.93		97.37		83.84		73.39

STEP TIME = 7.760 MIN ASCENT TIME = 65.15 MIN TOTAL DIVE TIME = 125 MIN ASCENT RATE = 1.289 FT/MIN

DIVE 1 STEP 25 PRIOR DEPTH = 130.00 THIS DEPTH = 120.00 GAS MIXTURE
 21.0 PCT
 79.0 PCT
 0.0 PCT

	SAFE	1	2	242.00	3	222.00	4	204.00	5	200.00	6	198.00	7	186.00	8	173.00	9	
TOTAL INERT	266.00			128.10		138.76		171.79		204.00		159.24		137.86		121.87		109.69
NITROGEN	127.88			130.11		116.30		87.00		60.42		49.58		43.87		40.36		38.00
HELIUM	.22			8.65		55.49		117.00		126.29		109.66		94.00		81.51		71.69

STEP TIME = 8.134 MIN ASCENT TIME = 73.29 MIN TOTAL DIVE TIME = 133 MIN ASCENT RATE = 1.229 FT/MIN

DIVE 1 STEP 26 PRIOR DEPTH = 120.00 THIS DEPTH = 110.00 GAS MIXTURE
 21.0 PCT
 79.0 PCT
 0.0 PCT

	SAFE	1	2	228.00	3	209.00	4	192.00	5	188.00	6	186.00	7	175.00	8	163.00	9	
TOTAL INERT	251.00			119.81		128.82		157.67		192.00		181.72		157.20		137.50		109.87
NITROGEN	119.74			.07		124.04		116.41		91.10		64.45		52.82		46.52		39.92
HELIUM						4.79		41.27		100.90		117.28		104.38		90.58		69.94

STEP TIME = 8.545 MIN ASCENT TIME = 81.83 MIN TOTAL DIVE TIME = 142 MIN ASCENT RATE = 1.170 FT/MIN

DIVE 1 STEP 27 PRIOR DEPTH = 110.00 THIS DEPTH = 100.42 GAS MIXTURE
 21.0 PCT
 79.0 PCT
 0.0 PCT

	SAFE	1	2	214.59	3	196.54	4	180.50	5	176.50	6	174.50	7	164.46	8	153.42	9	
TOTAL INERT	236.63			111.89		119.82		145.11		180.50		176.50		154.87		136.06		109.85
NITROGEN	111.86			.02		117.19		114.49		93.60		67.66		55.56		48.81		41.63
HELIUM						2.63		30.61		86.91		108.84		99.31		87.26		68.22

STEP TIME = 8.615 MIN ASCENT TIME = 90.45 MIN TOTAL DIVE TIME = 150 MIN ASCENT RATE = 1.112 FT/MIN

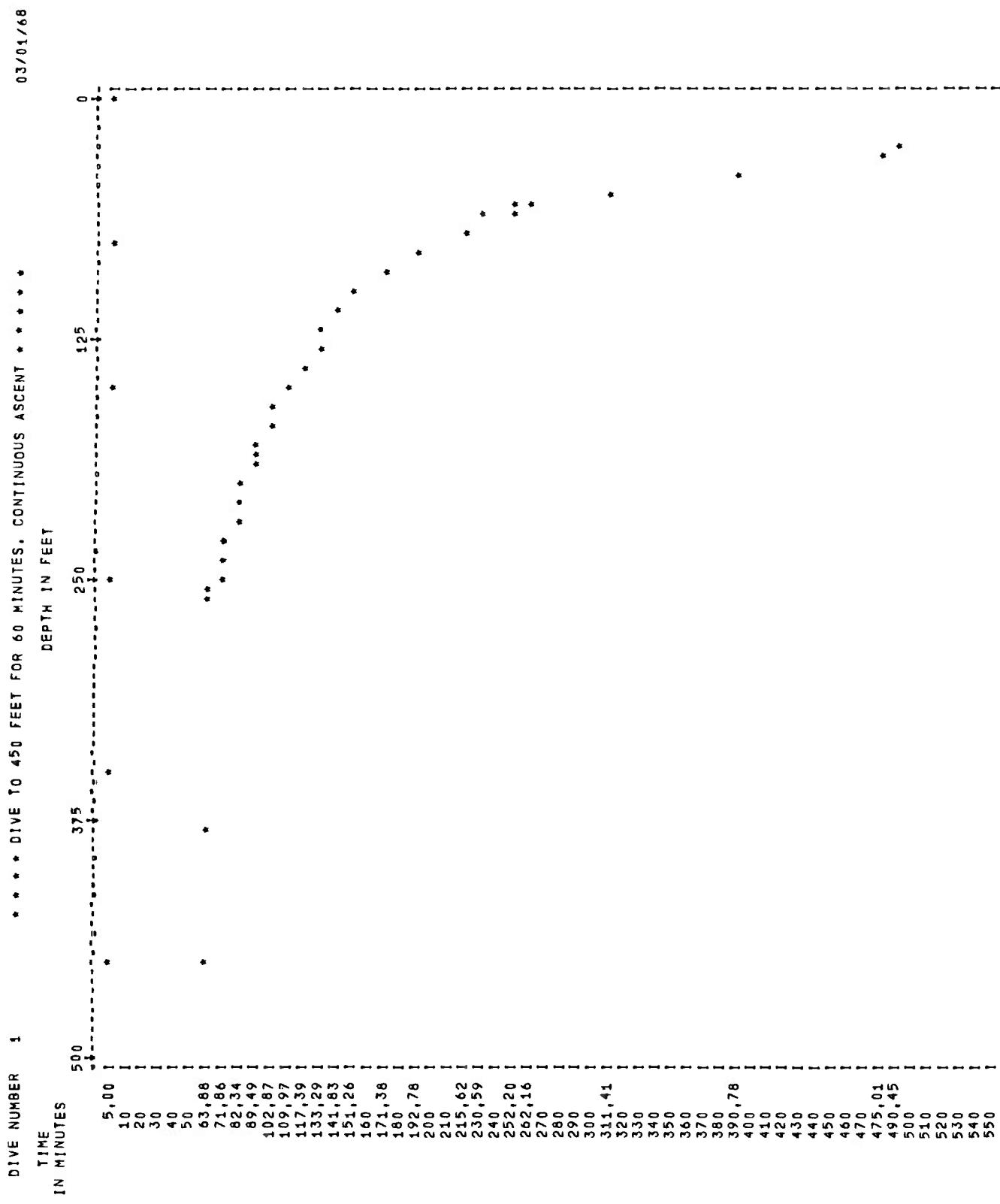
				OXYGEN NITROGEN HELIUM			
DIVE	STEP	PRIOR DEPTH =	THIS DEPTH =	PCT	PCT	PCT	PCT
		100.42	100.00	21.0	79.0	21.0	79.0
TISSUE PRESSURES							
SAFE	1	214.00	196.00	180.00	176.00	174.00	164.00
TOTAL INERT	111.18	119.02	142.00	179.45	176.00	154.63	135.97
NITROGEN	111.16	116.53	114.23	93.76	67.92	55.79	49.01
HELIUM	.02	2.49	29.76	85.69	108.08	98.84	86.95
STEP TIME =	1816 MIN	ASCENT TIME =	91.26 MIN	TOTAL DIVE TIME =	151 MIN	ASCENT RATE =	.513 FT/MIN
OXYGEN NITROGEN HELIUM							
DIVE	STEP	PRIOR DEPTH =	THIS DEPTH =	PCT	PCT	PCT	PCT
		100.00	90.00	21.0	79.0	21.0	79.0
TISSUE PRESSURES							
SAFE	1	200.00	183.00	168.00	164.00	162.00	153.00
TOTAL INERT	100.19	104.88	122.23	156.32	164.00	148.75	133.05
NITROGEN	100.19	104.26	107.41	95.85	73.21	60.75	53.36
HELIUM	.00	.62	14.82	60.46	90.79	88.00	79.70
STEP TIME =	20.120 MIN	ASCENT TIME =	111.38 MIN	TOTAL DIVE TIME =	171 MIN	ASCENT RATE =	.497 FT/MIN
OXYGEN NITROGEN HELIUM							
DIVE	STEP	PRIOR DEPTH =	THIS DEPTH =	PCT	PCT	PCT	PCT
		90.00	80.00	21.0	79.0	21.0	79.0
TISSUE PRESSURES							
SAFE	1	186.00	170.00	156.00	152.00	150.00	142.00
TOTAL INERT	91.94	91.12	106.78	136.69	152.00	142.29	129.52
NITROGEN	91.94	94.98	99.72	94.96	76.57	64.52	56.88
HELIUM	.00	.14	.06	41.73	75.43	77.77	72.64
STEP TIME =	21.394 MIN	ASCENT TIME =	132.78 MIN	TOTAL DIVE TIME =	193 MIN	ASCENT RATE =	.467 FT/MIN
OXYGEN NITROGEN HELIUM							
DIVE	STEP	PRIOR DEPTH =	THIS DEPTH =	PCT	PCT	PCT	PCT
		80.00	70.00	21.0	79.0	21.0	79.0
TISSUE PRESSURES							
SAFE	1	172.00	157.00	144.00	140.00	138.00	131.00
TOTAL INERT	83.85	86.52	94.75	119.81	140.00	135.23	125.35
NITROGEN	83.85	86.49	91.55	91.71	78.12	67.07	59.55
HELIUM	.00	.03	.52	28.09	61.88	68.16	65.80
STEP TIME =	22.840 MIN	ASCENT TIME =	155.62 MIN	TOTAL DIVE TIME =	216 MIN	ASCENT RATE =	.438 FT/MIN

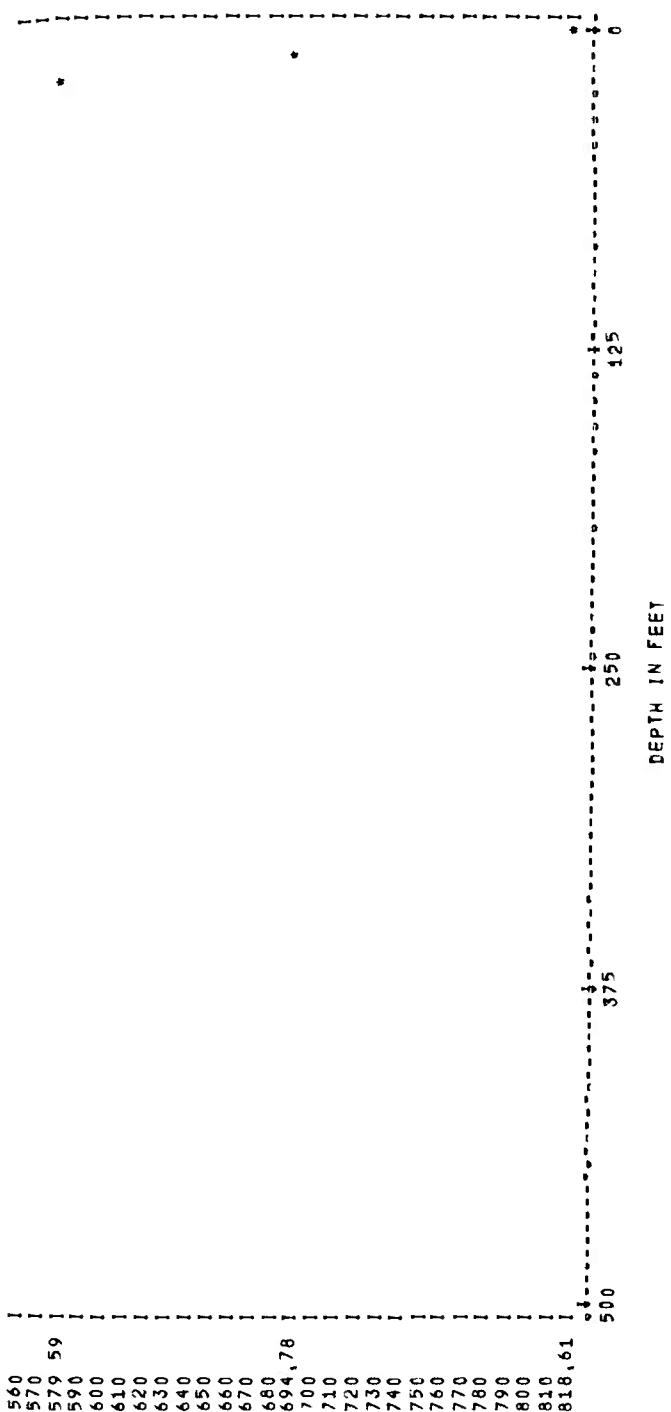
DIVE 1 STEP 32		PRIOR DEPTH = 70.00	THIS DEPTH = 63.80	GAS MIXTURE	OXYGEN NITROGEN HELIUM
		TISSUE PRESSURES			PCT PCT PCT
SAFE	181.70	1.63, 32 ²	148, 94 ³	136, 56 ⁴	132, 56 ^{**5**}
TOTAL INERT	78.85	81.34	88, 26	110, 44	132, 56 ^{130, 56}
NITROGEN	78.85	81.33	86, 35	88, 77	122, 43 ^{120, 56}
HELIUM	.00	.01	1.90	21, 67	68, 05 ^{68, 05}
STEP TIME = 14,974 MIN	ASCENT TIME = 170,59 MIN	TOTAL DIVE TIME = 231 MIN		ASCENT RATE = .414 FT/MIN	OXYGEN NITROGEN HELIUM
DIVE 1 STEP 33		PRIOR DEPTH = 63.80	THIS DEPTH = 60.00	GAS MIXTURE	PCT PCT PCT
		TISSUE PRESSURES			21.0 79.0 0.0
SAFE	176.00	1.58, 00 ¹	144, 00 ²	132, 00 ³	128, 00 ⁴
TOTAL INERT	75.06	77.10	82, 87	102, 39	125, 62 ^{126, 00}
NITROGEN	75.06	77.09	81, 73	85, 63	119, 48 ^{126, 00}
HELIUM	.00	.00	1.14	16, 76	68, 62 ^{68, 62}
STEP TIME = 14,820 MIN	ASCENT TIME = 185,41 MIN	TOTAL DIVE TIME = 245 MIN		ASCENT RATE = .257 FT/MIN	OXYGEN NITROGEN HELIUM
DIVE 1 STEP 34		PRIOR DEPTH = 60.00	THIS DEPTH = 58.30	GAS MIXTURE	PCT PCT PCT
		TISSUE PRESSURES			21.0 79.0 0.0
SAFE	173.44	1.55, 61 ¹	141, 78 ²	129, 95 ³	123, 95 ⁴
TOTAL INERT	73.62	75.47	80, 76	99, 11	122, 60 ^{123, 95}
NITROGEN	73.62	75.47	79, 86	84, 21	118, 13 ^{118, 13}
HELIUM	.00	.00	.90	14, 90	68, 78 ^{68, 78}
STEP TIME = 6,788 MIN	ASCENT TIME = 192,20 MIN	TOTAL DIVE TIME = 252 MIN		ASCENT RATE = .251 FT/MIN	OXYGEN NITROGEN HELIUM
DIVE 1 STEP 35		PRIOR DEPTH = 58.30	THIS DEPTH = 56.50	GAS MIXTURE	PCT PCT PCT
		TISSUE PRESSURES			21.0 79.0 0.0
SAFE	170.75	1.53, 10 ¹	139, 45 ²	127, 80 ³	123, 80 ⁴
TOTAL INERT	71.86	73.41	78, 02	94, 72	118, 37 ^{121, 02}
NITROGEN	71.86	73.41	77, 39	82, 18	116, 15 ^{121, 02}
HELIUM	.00	.00	.64	12, 54	77, 02 ^{68, 93}
STEP TIME = 9,960 MIN	ASCENT TIME = 202,16 MIN	TOTAL DIVE TIME = 262 MIN		ASCENT RATE = .180 FT/MIN	OXYGEN NITROGEN HELIUM

				OXYGEN NITROGEN HELIUM			
DIVE	STEP	PRIOR DEPTH =	THIS DEPTH =	PCT	PCT	PCT	PCT
TISSUE PRESSURES							
SAFE	1	144.00	131.00	3	4	5	6
TOTAL INERT	66.33	67.12	69.36	79.25	100.86	107.89	109.00
NITROGEN	66.73	67.32	69.25	73.91	73.87	68.70	63.46
HELIUM	.00	.00	.12	5.34	26.98	39.19	43.45
STEP TIME = 49.254 MIN	ASCENT TIME = 251.41 MIN	TOTAL DIVE TIME = 311 MIN	ASCENT RATE = .132 FT/MIN	GAS MIXTURE			
OXYGEN NITROGEN HELIUM							
DIVE	STEP	PRIOR DEPTH =	THIS DEPTH =	PCT	PCT	PCT	PCT
TISSUE PRESSURES							
SAFE	1	146.00	130.00	2	3	4	5
TOTAL INERT	58.38	59.09	60.58	65.40	104.00	102.00	98.00
NITROGEN	58.38	59.09	60.57	64.05	67.55	65.98	62.85
HELIUM	.00	.00	.01	1.35	13.57	24.78	30.81
STEP TIME = 79.365 MIN	ASCENT TIME = 330.78 MIN	TOTAL DIVE TIME = 391 MIN	ASCENT RATE = .126 FT/MIN	GAS MIXTURE			
OXYGEN NITROGEN HELIUM							
DIVE	STEP	PRIOR DEPTH =	THIS DEPTH =	PCT	PCT	PCT	PCT
TISSUE PRESSURES							
SAFE	1	131.00	116.00	2	3	4	5
TOTAL INERT	50.44	51.11	52.47	55.70	96.00	92.00	90.00
NITROGEN	50.44	51.11	52.46	55.39	60.12	60.12	59.98
HELIUM	.00	.00	.00	.31	6.54	15.23	21.39
STEP TIME = 84.228 MIN	ASCENT TIME = 415.01 MIN	TOTAL DIVE TIME = 475 MIN	ASCENT RATE = .119 FT/MIN	GAS MIXTURE			
OXYGEN NITROGEN HELIUM							
DIVE	STEP	PRIOR DEPTH =	THIS DEPTH =	PCT	PCT	PCT	PCT
TISSUE PRESSURES							
SAFE	1	128.35	113.53	2	3	4	5
TOTAL INERT	49.04	49.70	51.14	54.14	93.88	89.88	87.88
NITROGEN	49.04	49.70	51.04	53.90	64.46	74.03	79.28
HELIUM	.00	.00	.00	.24	5.72	13.93	20.00
STEP TIME = 15.441 MIN	ASCENT TIME = 430.45 MIN	TOTAL DIVE TIME = 490 MIN	ASCENT RATE = .114 FT/MIN	GAS MIXTURE			

DIVE NUMBER 1 * * * DIVE TO 450 FEET FOR 60 MINUTES, CONTINUOUS ASCENT * * * * 03/01/68

STEP	TIME MIN	DEPTH FEET	CUMULATIVE TIME			OXYGEN NITROGEN HELIUM		
			H	M	S	PCT	PCT	PCT
0	0	0	0	0	0	01.0	79.0	0.0
1	1	0	0	0	0	01.1	79.0	0.0
2	1	75	0	0	0	01.2	4.0	96.0
3	1	150	0	0	0	01.3	4.0	96.0
4	1	225	0	0	0	01.4	4.0	96.0
5	1	300	0	0	0	01.4	4.0	96.0
6	55	350	0	0	0	01.5	4.0	96.0
7	0	450	0	0	0	01.6	4.0	96.0
8	1	450	0	0	0	01.7	4.0	96.0
9	2	380	0	0	0	01.8	4.0	96.0
10	1	260	0	0	0	01.9	4.0	96.0
11	1	255	0	0	0	01.9	4.0	96.0
12	2	250	0	0	0	01.9	4.0	96.0
13	3	240	0	0	0	01.9	4.0	96.0
14	3	230	0	0	0	01.9	4.0	96.0
15	3	220	0	0	0	01.9	4.0	96.0
16	4	210	0	0	0	01.9	4.0	96.0
17	3	200	0	0	0	01.9	4.0	96.0
18	4	190	0	0	0	01.9	4.0	96.0
19	3	185	0	0	0	01.9	4.0	96.0
20	7	185	0	0	0	01.9	4.0	96.0
21	7	170	0	0	0	01.9	4.0	96.0
22	7	160	0	0	0	01.9	4.0	96.0
23	7	150	0	0	0	01.9	4.0	96.0
24	8	140	0	0	0	01.9	4.0	96.0
25	8	130	0	0	0	01.9	4.0	96.0
26	9	120	0	0	0	01.9	4.0	96.0
27	9	110	0	0	0	01.9	4.0	96.0
28	1	100	0	0	0	01.9	4.0	96.0
29	20	100	0	0	0	01.9	4.0	96.0
30	21	90	0	0	0	01.9	4.0	96.0
31	23	80	0	0	0	01.9	4.0	96.0
32	15	70	0	0	0	01.9	4.0	96.0
33	15	64	0	0	0	01.9	4.0	96.0
34	7	60	0	0	0	01.9	4.0	96.0
35	10	58	0	0	0	01.9	4.0	96.0
36	49	57	0	0	0	01.9	4.0	96.0
37	37	50	0	0	0	01.9	4.0	96.0
38	84	40	0	0	0	01.9	4.0	96.0
39	15	30	0	0	0	01.9	4.0	96.0
40	89	28	0	0	0	01.9	4.0	96.0
41	115	20	0	0	0	01.9	4.0	96.0
42	124	10	0	0	0	01.9	4.0	96.0





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13 ABSTRACT

A digital computer program for calculating either continuous ascent or stop type decompression schedules is described, and examples of applications are given. The formulas used for continuous ascent were obtained analytically as solutions of differential equations relating the inert gas tension in the current critical tissue to the safe depth and with the actual depth kept equal to the safe depth at all times after an initial fast rise from the bottom to the safe depth. Thus the rate of decompression of the critical tissue controls the rate of ascent. Gas tensions in nine tissues having the same range of gas exchange half-times as have been used in EDU reports are calculated on a continuous basis, with the one having the deepest safe depth being the current critical tissue. The stop type ascent portion of the program may be used to generate a staged ascent using the same parameters for comparison with the continuous ascent schedule. The starting conditions for ascent may either be computed by the program from the dive history or be communicated to it as a subroutine in connection with another program. The program may be used either to prescribe ascent schedules or to analyze dives for which the history is known.

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14 KEY WORDS	LINK A		LINK B		LINK C	
	ROLE	WT	ROLE	WT	ROLE	WT
Decompression schedules Continuous ascent Computer, digital Inert gas exchange						